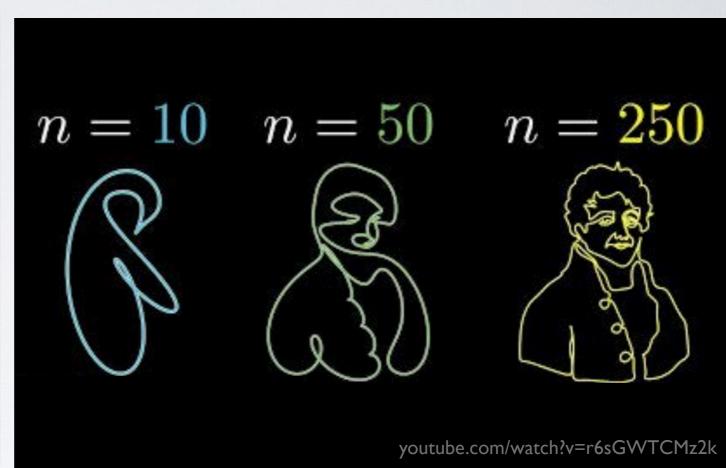
Week 9 - #1

Fourier Series and Transforms (I)





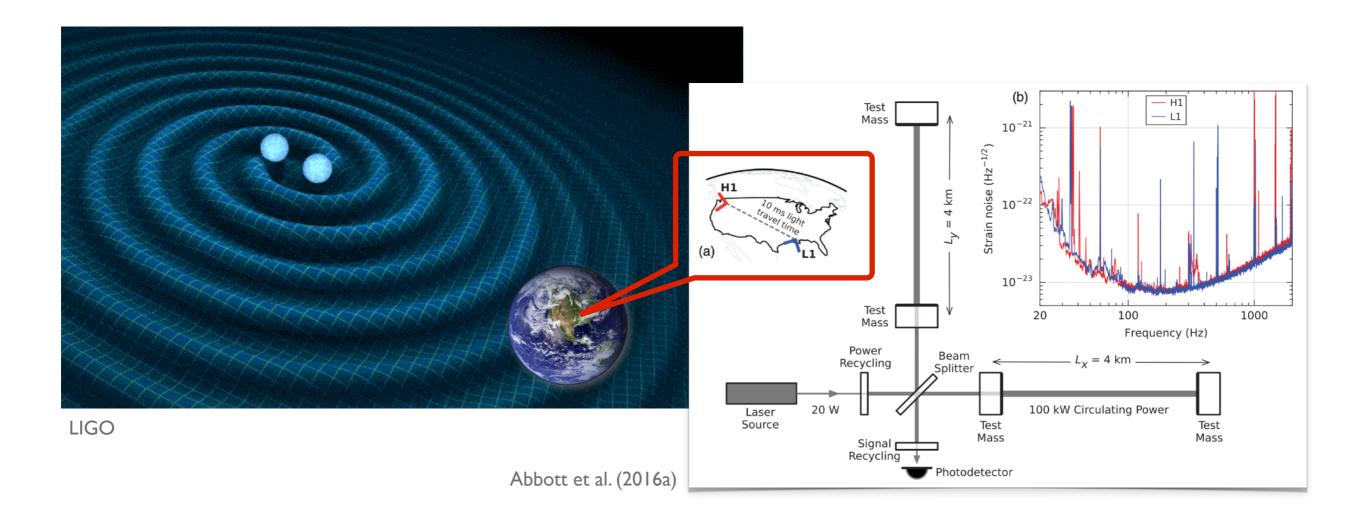
Today: Ch 7

Next Class: Ch 7

Ji-hoon Kim (Seoul National University)

— [open book and open note, but no cellphone or laptop, drop it off as you leave the class] —

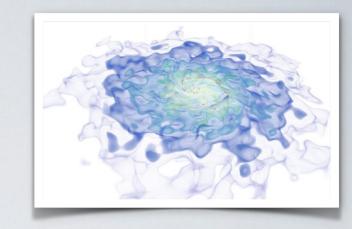
- 1. Boas, Chapter 7, Section 3, Problem 5 (see p.345/373 for definitions of *fundamentals & overtones*)
- 2. Boas, Chapter 7, Section 4, Problem 2 (which allows us to trivially prove Eq.(4.8) in p.349)



Rudimentary Mathematical Methods of Physics (Fall 2025): Suggested Problems in Chapter 7, Boas, 3rd ed.

The problems I suggest you to take a deeper look into include, but are not limited to, the following. The class homework assignments will mainly be from this list.

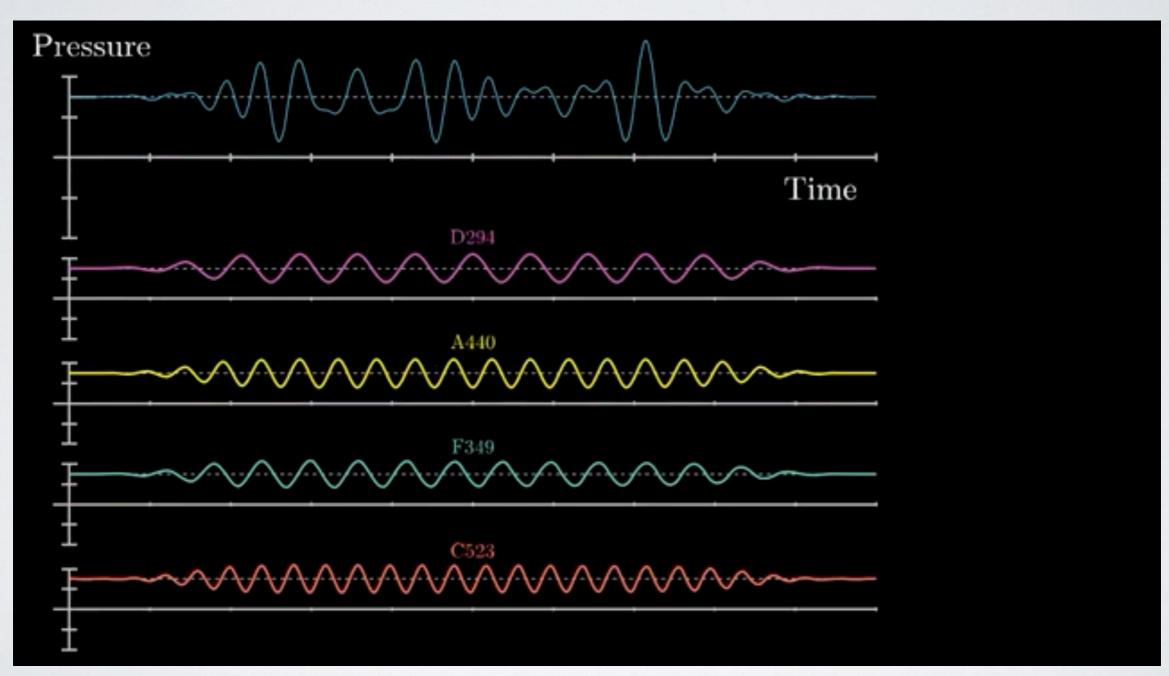
- Section 02: Problems 12, 17
- Section 03: Problems 8
- Section 04: Problems 1, 13, 16
- Section 05: Problems 1, 3, 4, 7, 9, 11
- Section 06: Problems 10, 12 (for Problem 5.7 and 5.9), 14, 15
- Section 07: Problems 7, 9, 11, 13
- Section 08: Problems 2, 14, 15(a)(b), 20
- Section 09: Problems 9, 10, 11, 19, 20, 23
- Section 10: Problems 2
- Section 11: Problems 6, 8
- Section 12: Problems 6, 9, 10, 15, 18, 21, 23, 26, 31, 35
- Section 13: Problems 4, 8, 14, 23



Fourier Series

Fourier Series

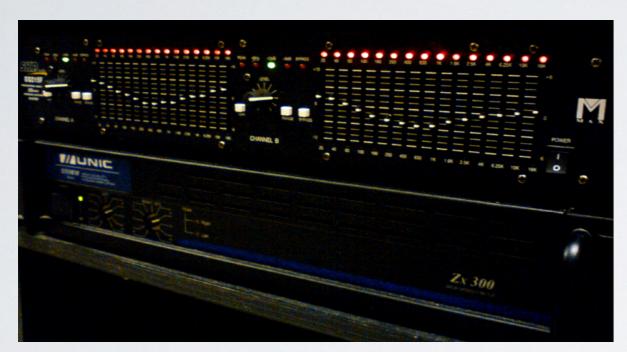
A visualization of Fourier series.



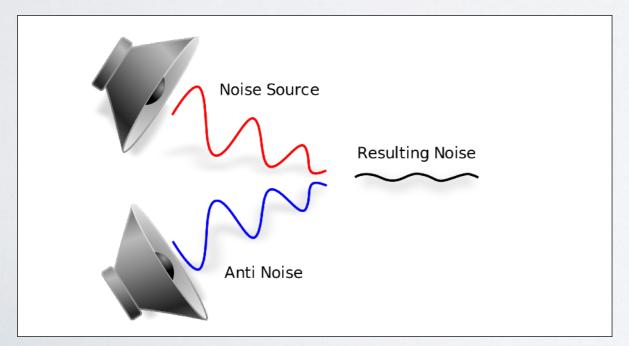
youtube.com/watch?v=spUNpyF58BY

Applications of Fourier Analysis

• Whenever there are wave patterns.



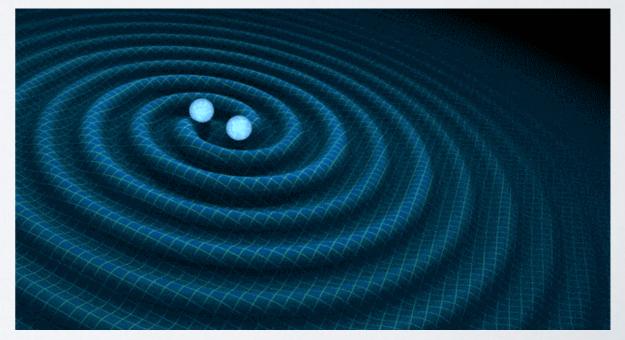
Sound equalizer, Wikipedia commons



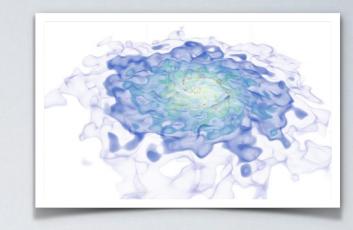
Active noise cancelling, Wikipedia commons



Electroencephalography (EEG), abcnews.go.com



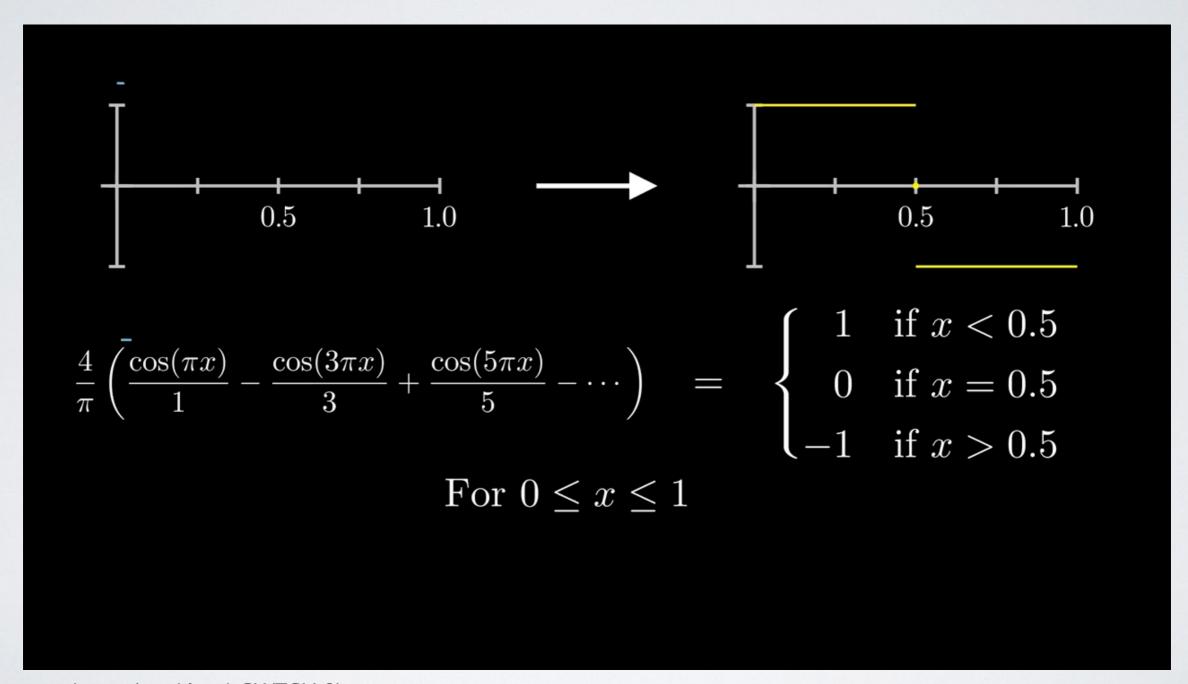
LIGO



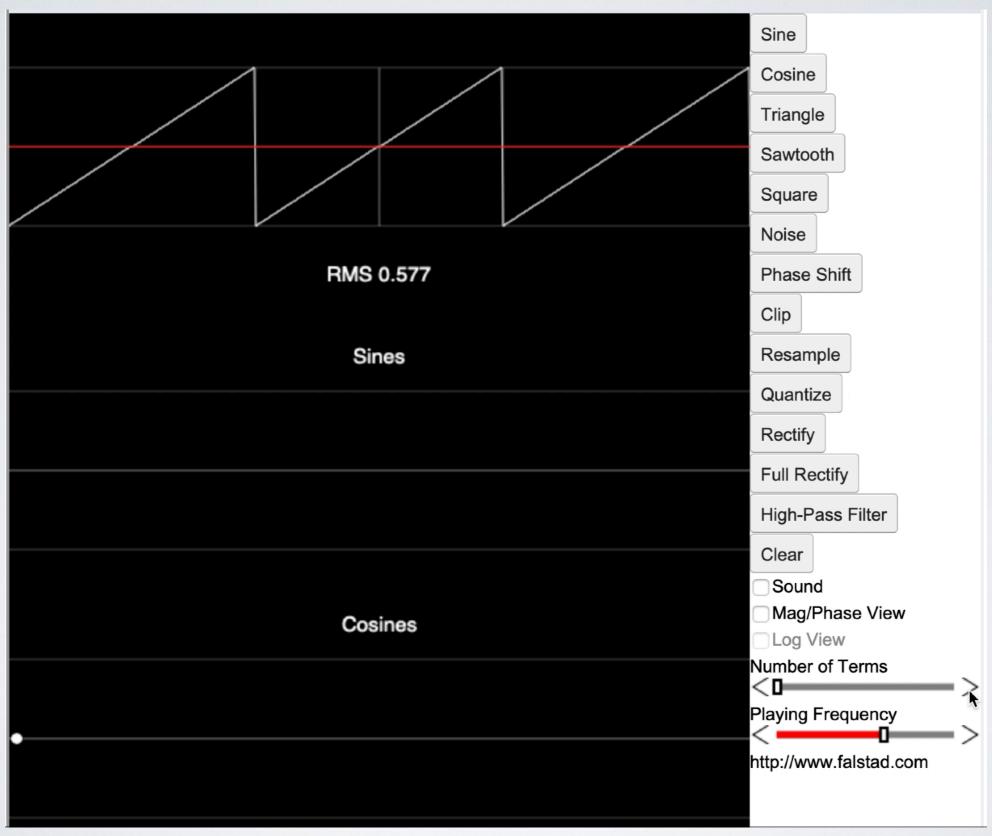
Sine-Cosine Fourier Series

Fourier Cosine Series

• A visualization of Fourier cosine series.

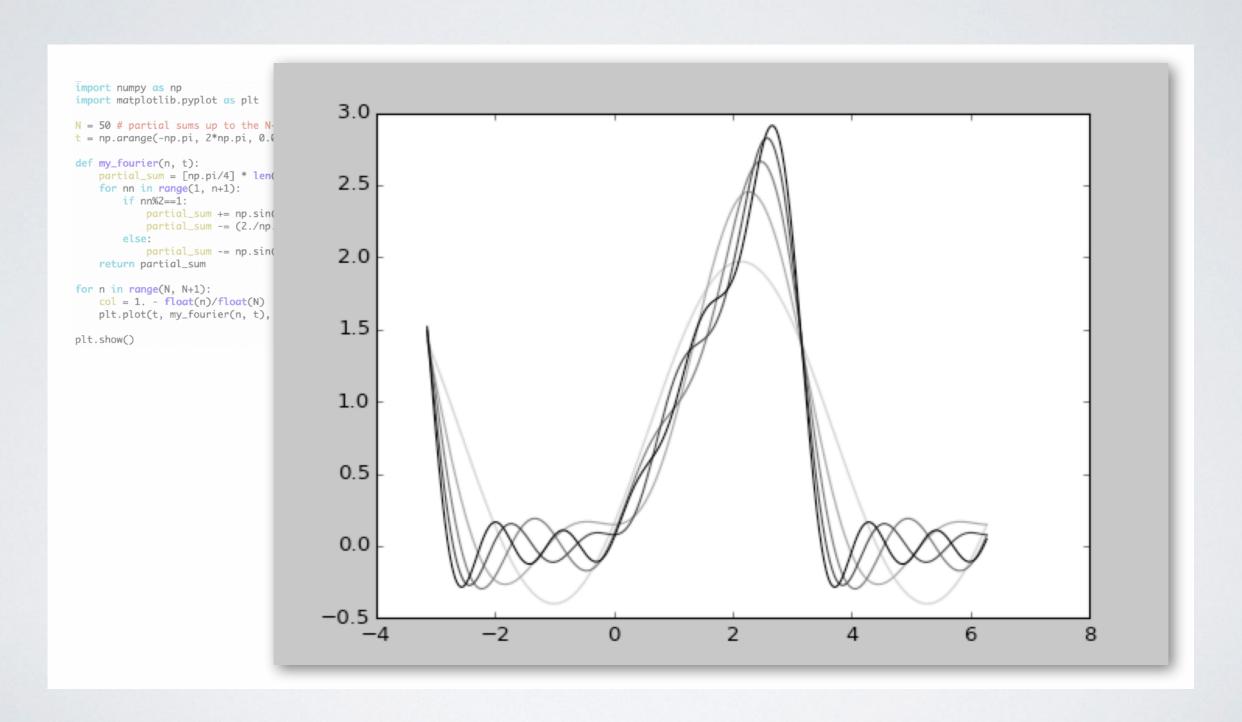


Fourier Sine Series



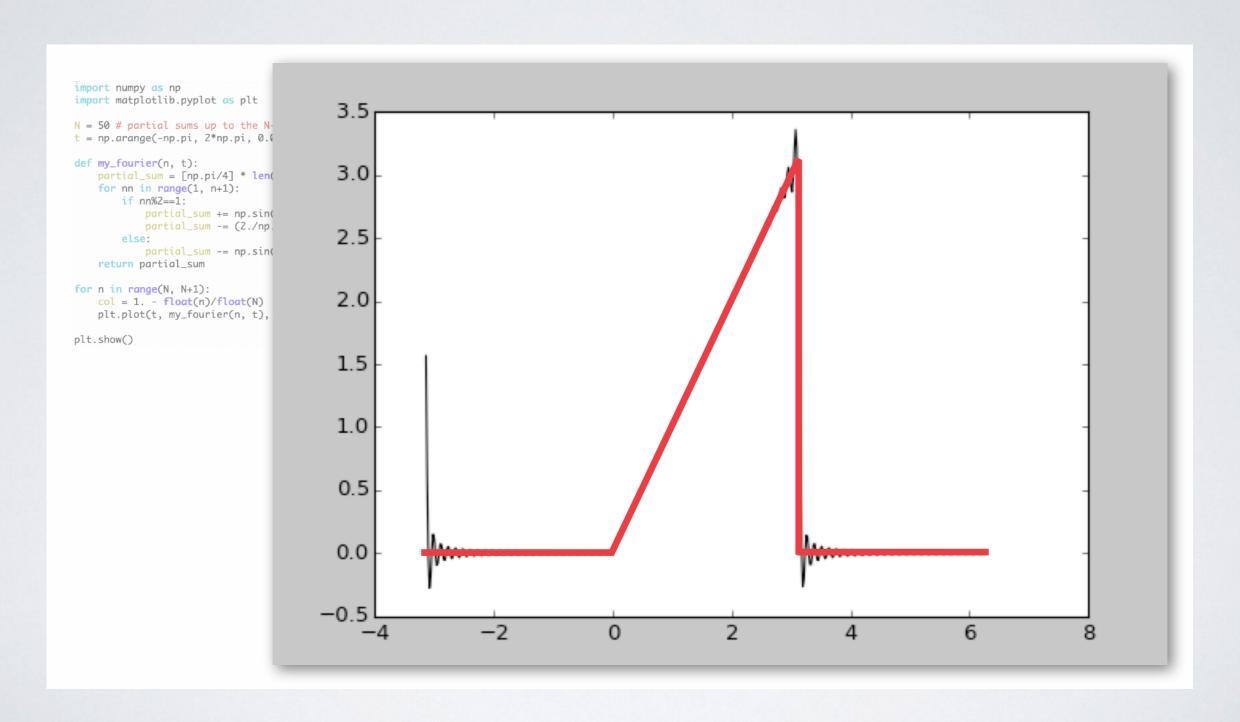
Sine-Cosine Fourier Series

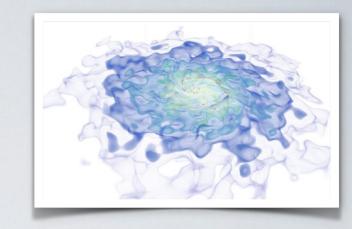
• A visualization of sine-cosine Fourier series (Ch 7.5, Prob 5.7).



Sine-Cosine Fourier Series

• A visualization of sine-cosine Fourier series (Ch 7.5, Prob 5.7).

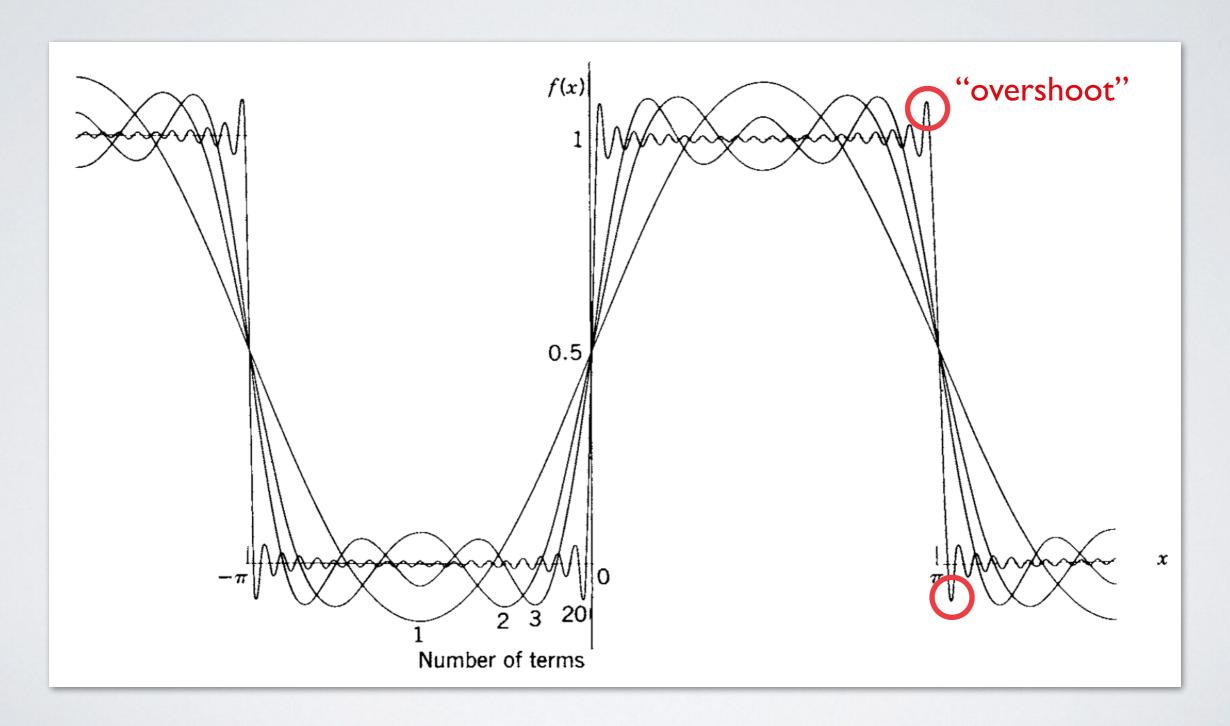




Gibbs Phenomenon

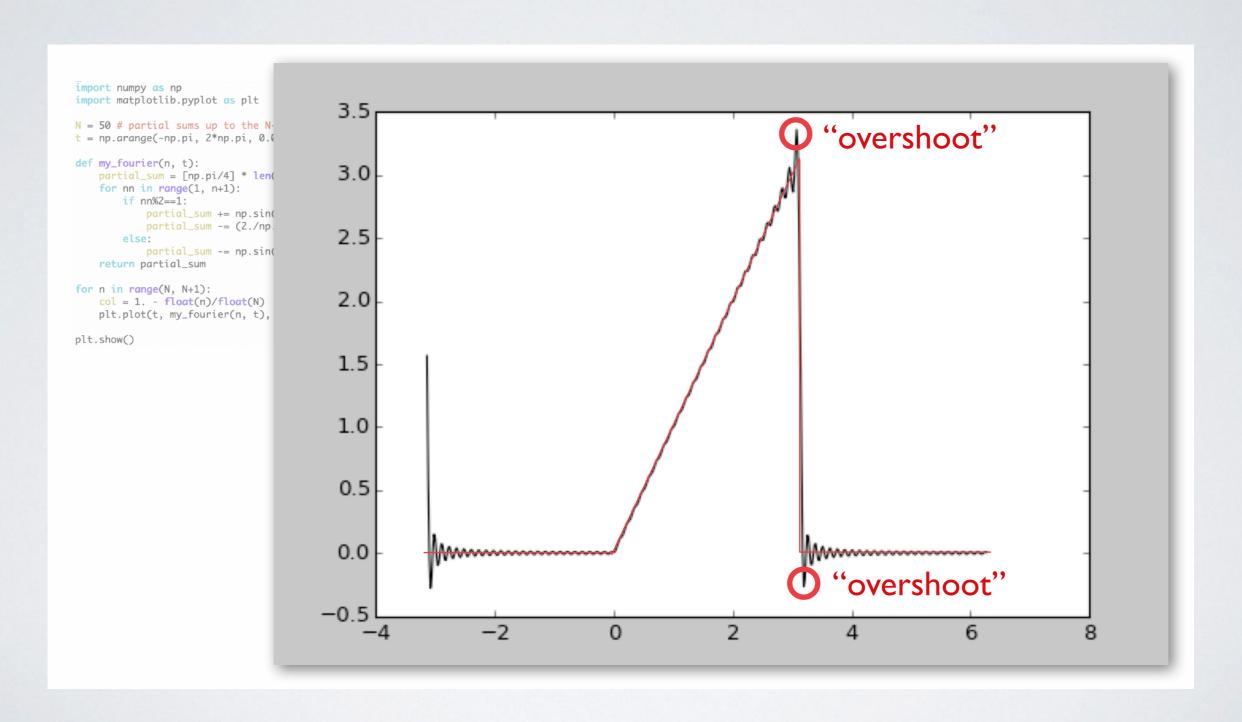
Fourier Sine Series

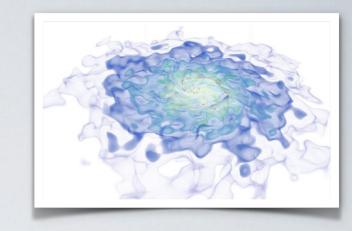
• A visualization of Fourier sine series (Ch 7.6, Figure 6.2).



Sine-Cosine Fourier Series

• A visualization of sine-cosine Fourier series (Ch 7.5, Prob 5.7).

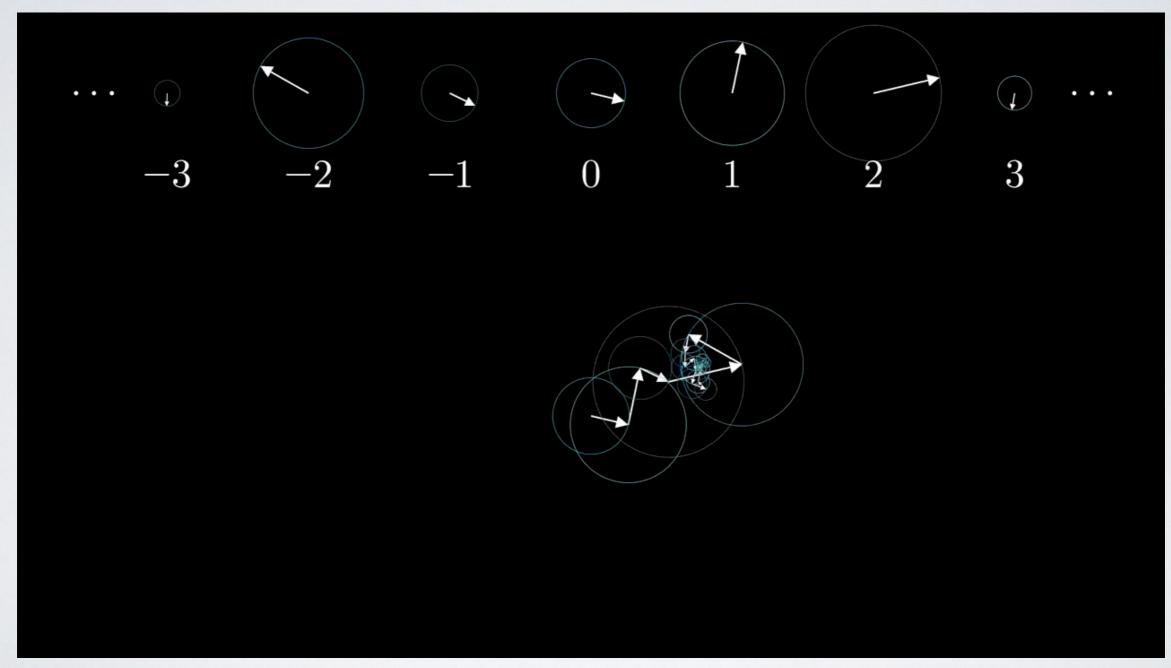




Complex Fourier Series

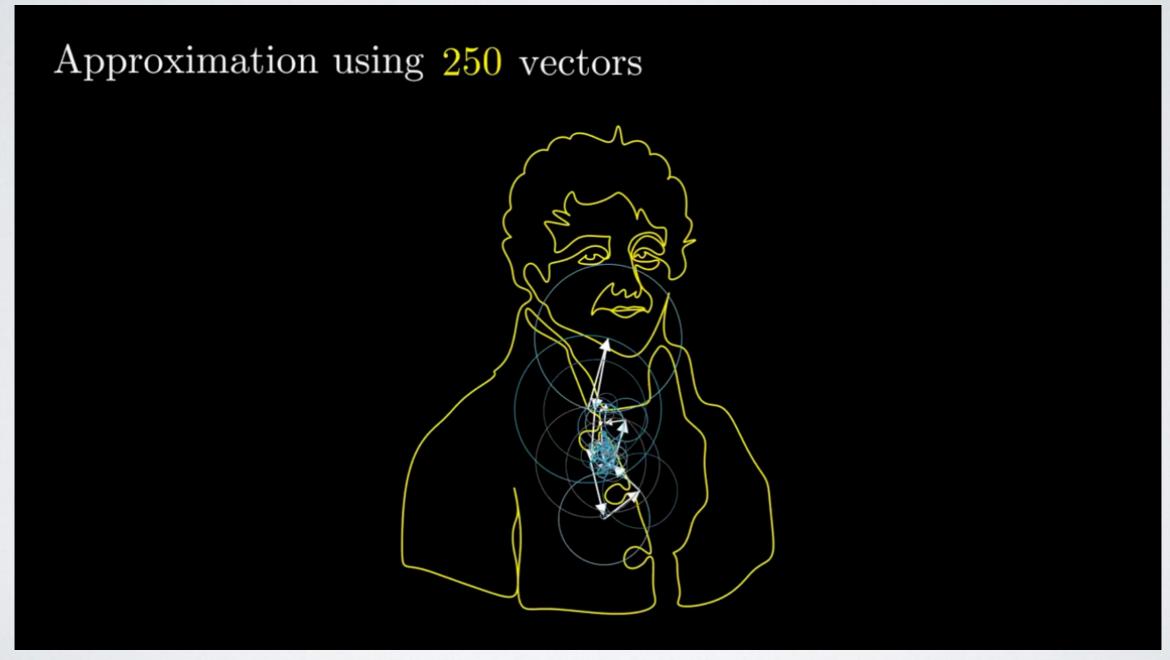
Complex Fourier Series

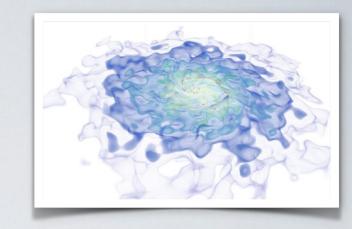
A visualization of complex Fourier series.



Complex Fourier Series

A visualization of complex Fourier series.



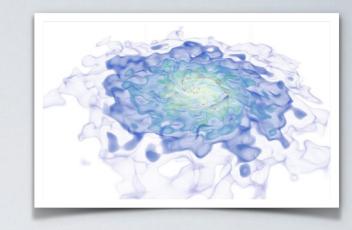


Grading Scheme

Grade policy in the course syllabus.

| * 3. 평가방법 | 구분 | 출석 | 과제 | 중간 | 기말 | 수시평가 | 태도 | 기타 | 합계 |
|-----------|---|----|----|------|------|------|----|----|-----|
| | 비율 | 5 | 35 | 20 | 20 | 15 | 5 | 0 | 100 |
| | 비고 | | | 지필고사 | 지필고사 | | | | |
| | 출석 규정 : 수업일수의 1/3을 초과하여 결석하면 성적은 "F" 또는 "U"가 됨(학칙 85조) (담당교수가 불가피한 결석으로 인정하는 경우는 예외로 할 수 있음) | | | | | | | | |

- 6 HW assignments Scheduled in 3, 5, 7, 10, 12, 14th week
 - Due in < I weeks on eTL or in the classroom
 - Only handwritten answers accepted (except numerical problems)
- Term project paper Due near the end of the semester
 - To be discussed in detail later

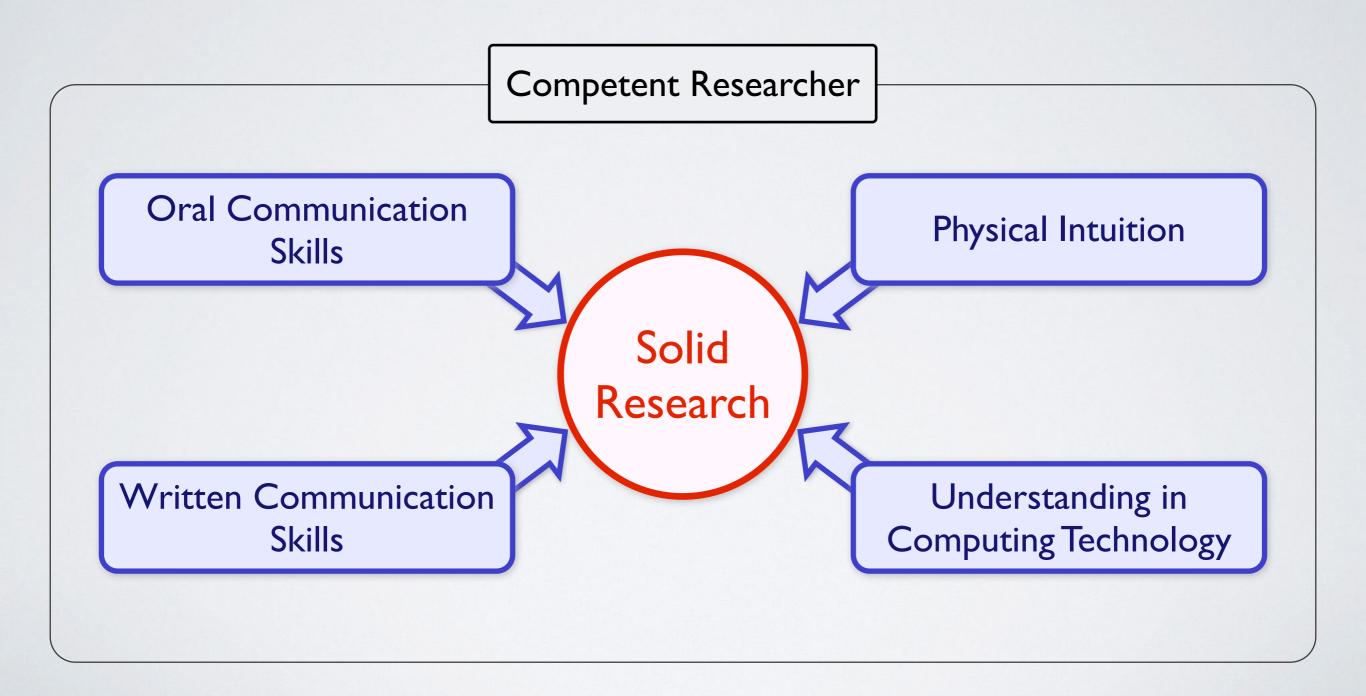


Essential Skillsets For Future Physicists & Astrophysicists

(on top of the strong physics/math background you will build)

Essential Skillsets For (Astro)Physicists

• To become proficient and effective researchers while relying less on guesswork as you navigate through the academia



Essential Skillsets For (Astro)Physicists

Competent Researcher

Oral Communication Skills

- How to present long and short talks
- How to answer questions
- How to make an elevator pitch

Physical Intuition

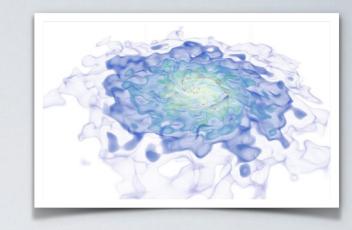
Solid Research

Understanding in Computing Technology

Written Communication Skills

- How to write papers and proceedings
- How to write referee reports
- How to respond to referee reports

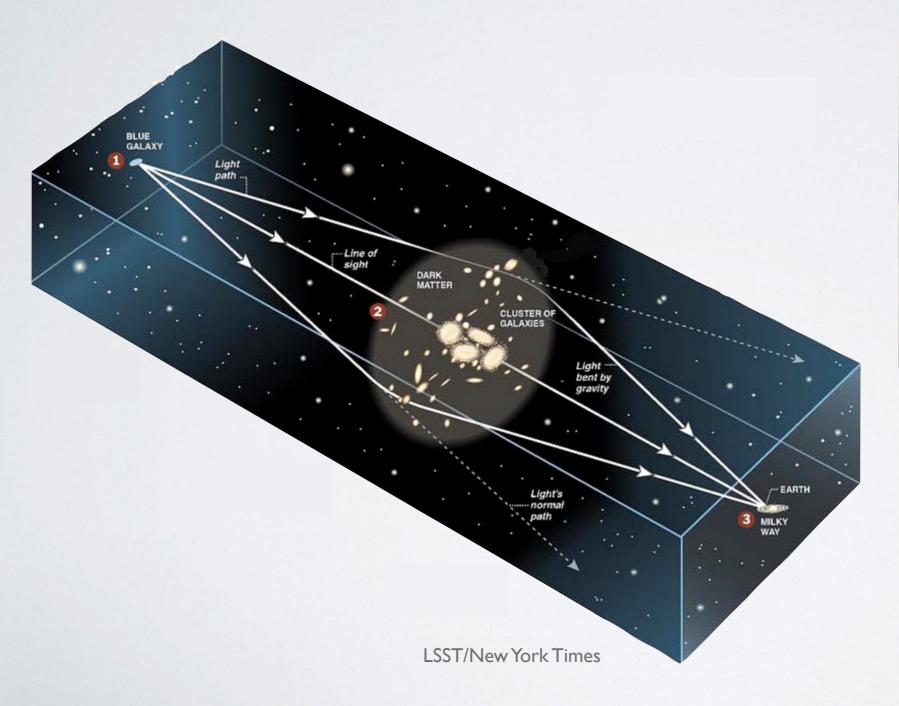




My Examples This Semester

Gravitational Lens As A Telescope

• Galaxy clusters act as nature-made cosmic telescopes allowing us to observe the young Universe (~10 to 10³ times magnified).

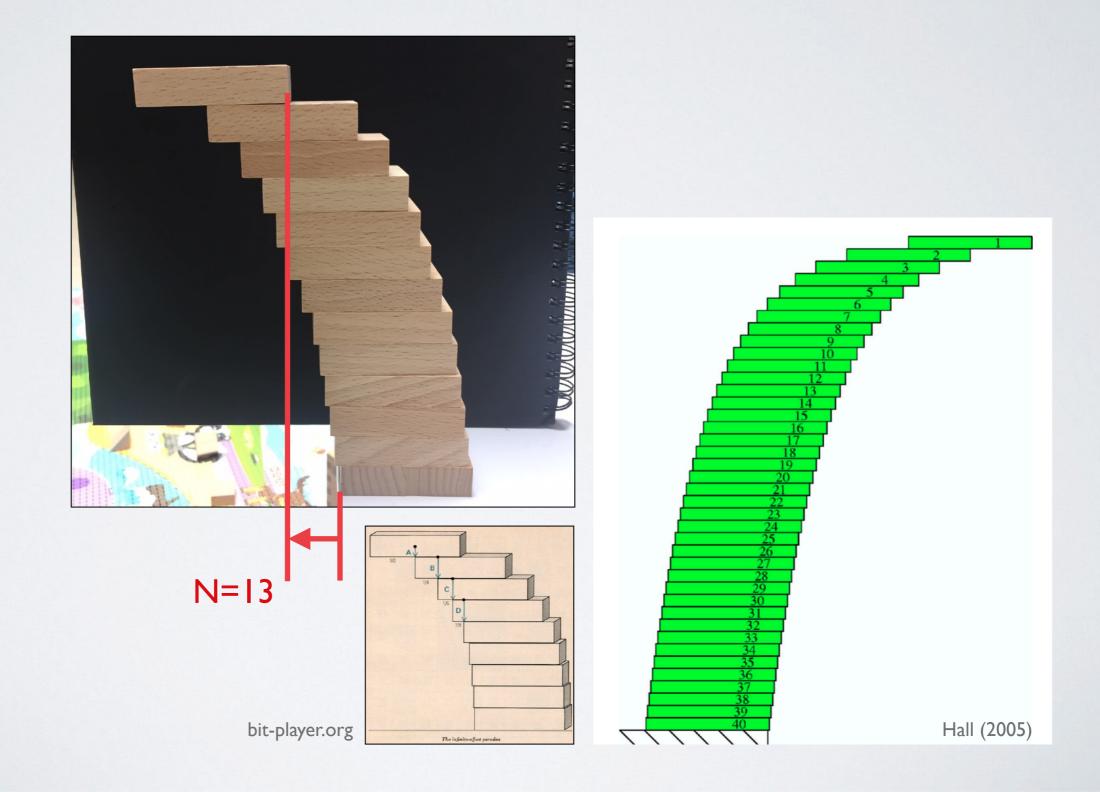




Marshall

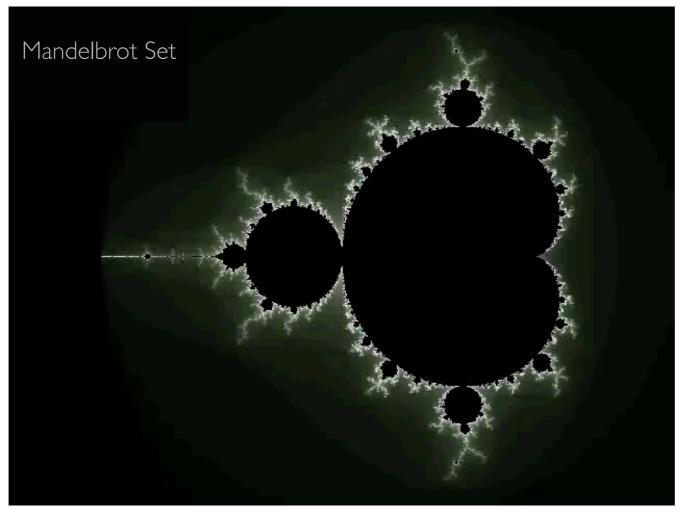
Fun with Stacking Blocks

• See: Problem 16.1 + "Fun with Stacking Blocks" (Hall, 2005), etc.



— [open book and open note, "and" cellphone or laptop, drop it off as you leave the class] —

- 1. Define "complex plane" from your textbook; then, Boas, Chapter 2, Section 5, Problem 59
- 2. Briefly explain the so-called Mandelbrot set demonstrated in the following movie in particular, how this one of the most famous images in the fractal/chaos theory is plotted on a "complex plane".



youtube.com/watch?v=G_GBwuYuOOs, Mandelbrot set on complex plane

— [open book and open note, "and" cellphone or laptop, drop it off as you leave the class] —

- 1. Boas, Chapter 3, Section 11, Problem 22
- 2. Study and briefly explain how matrix operations are used in 3-dimensional rendering in various fields such as game design, immersive visualization, augmented reality, and others.





www.techspot.com/article/1857-how-to-3d-rendering-vertex-processing

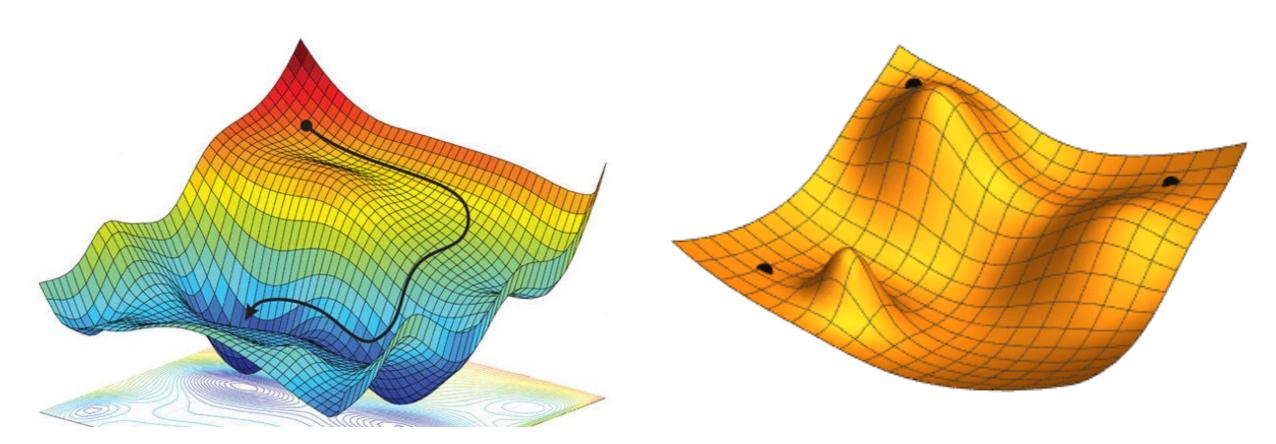
— [open book and open note, "and" cellphone or laptop, drop it off as you leave the class] —

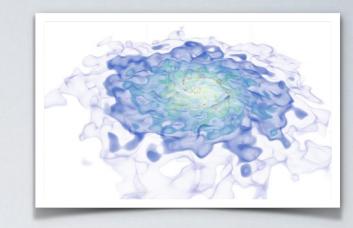
- 1. Explain in layman's terms as if you do to your friend in the College of Humanities what a tensor is. Study and briefly explain how the "tensors" are used in machine learning. For example, the popular open source deep neural network platform by Google is called TensorFlow.
- 2. Boas, Chapter 10, Section 5, Problem 11



— [open book and open note, "and" cellphone or laptop, drop it off as you leave the class] —

- 1. Boas, Chapter 5, Section 3, Problem 24
- 2. Explain in layman's terms what the figure/movie below are trying to visualize by using the term "gradient". On a related note, study and explain briefly how the concept of "gradient" is used in machine learning and artificial intelligence.





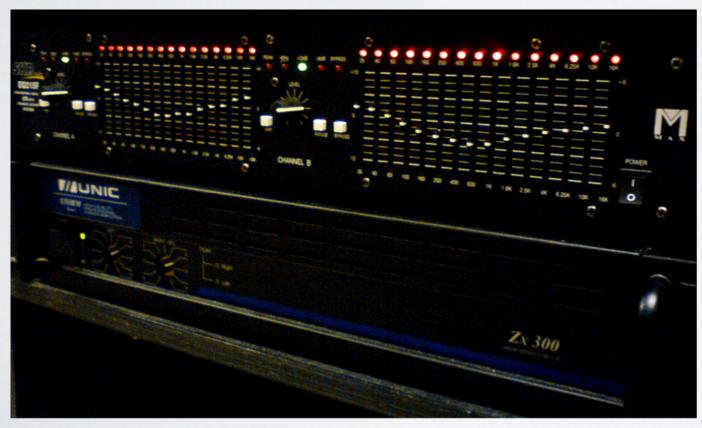
Project Ideas

- Report about mathematical physics ideas or methodology being used in contemporary physics research or in daily applications.
- Due: Beginning of the class on Dec. 1st
 (10 page-limit including cover/reference; typewritten report okay)



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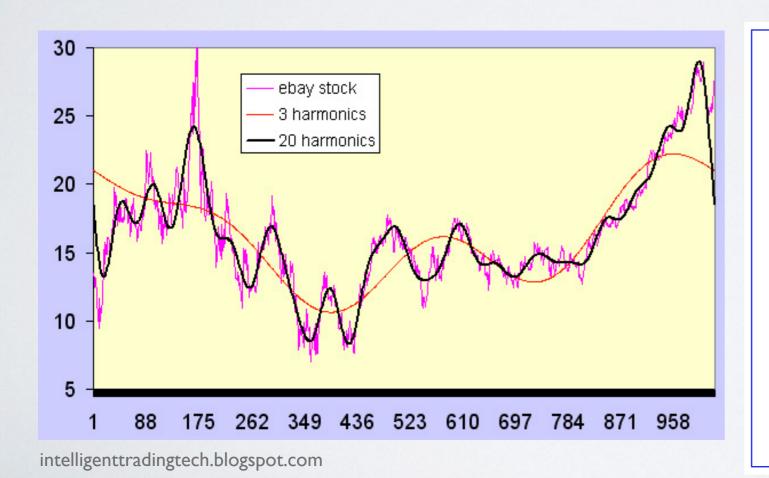
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Sound equalizer, Wikipedia commons

- 0: no paper found with your name on it
- I: paper found with your name on it
- 2: some scribbles
- 3: reasonable problem & solution
- 4: unique, interesting problem & solution
- 5: reserved for those exceptional

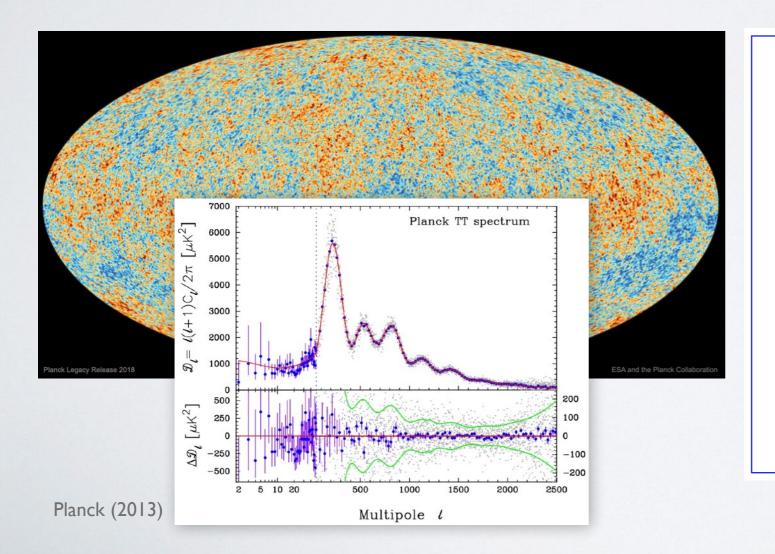
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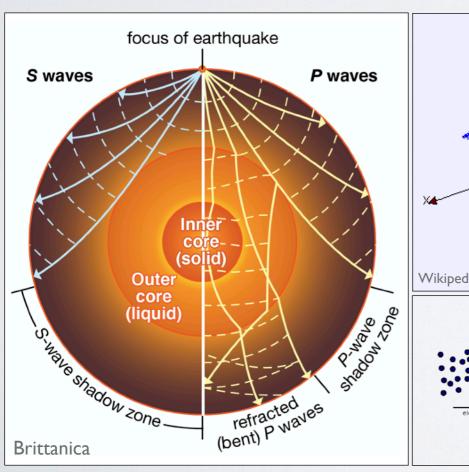


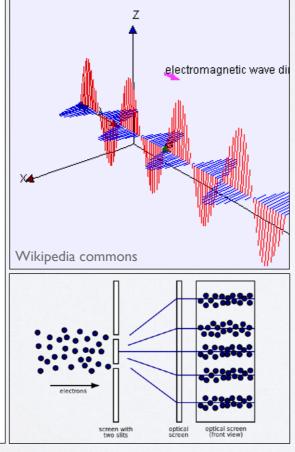
theatlantic.com

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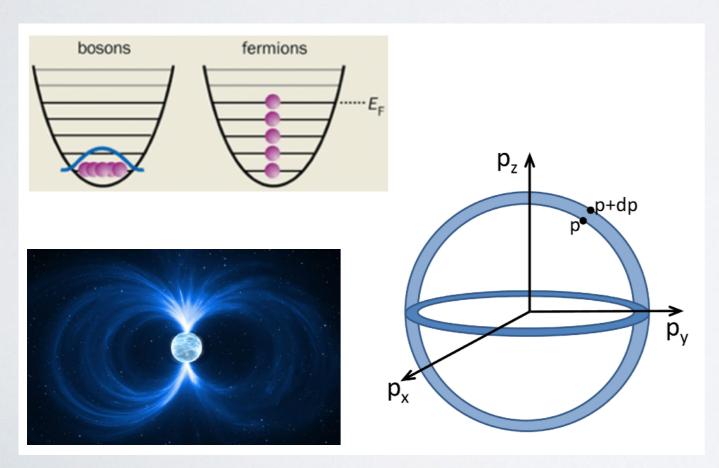
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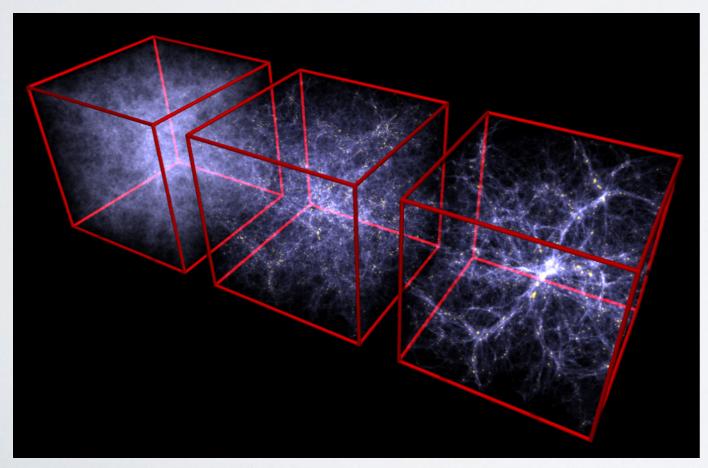


Spherical shell in momentum space (Parker, 2016), phyiscsworld.com, medium.com

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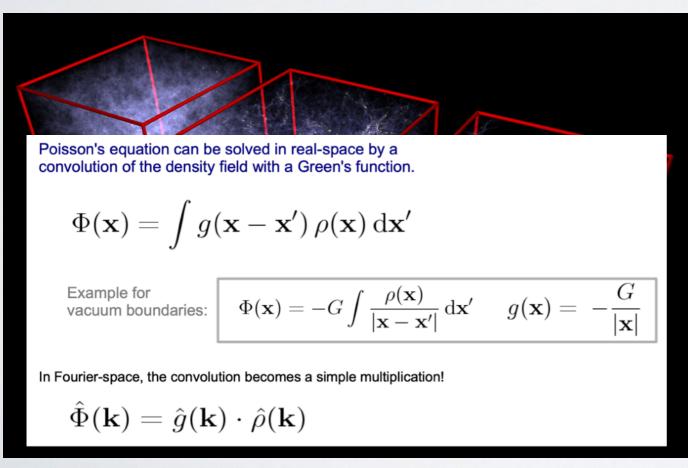
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TensorFlow

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Article Discovering faster matrix multiplication algorithms with reinforcement learning https://doi.org/10.1038/s41586-022-05172-4 Alhussein Fawzi^{1,2™}, Matej Balog^{1,2}, Aja Huang^{1,2}, Thomas Hubert^{1,2}, Bernardino Romera-Paredes^{1,2}, Mohammadamin Barekatain¹, Alexander Novikov¹, Received: 2 October 2021 Francisco J. R. Ruiz¹, Julian Schrittwieser¹, Grzegorz Swirszcz¹, David Silver¹, Demis Hassab Accepted: 2 August 2022 Published online: 5 October 2022 Improving the efficiency of algorithms for fundamental computations can have a widespread impact, as it can affect the overall speed of a large amount of computations. Check for updates Matrix multiplication is one such primitive task, occurring in many systems-from neural networks to scientific computing routines. The automatic discovery of algorithms using machine learning offers the prospect of reaching beyond human

Grading guideline

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deepmind.com

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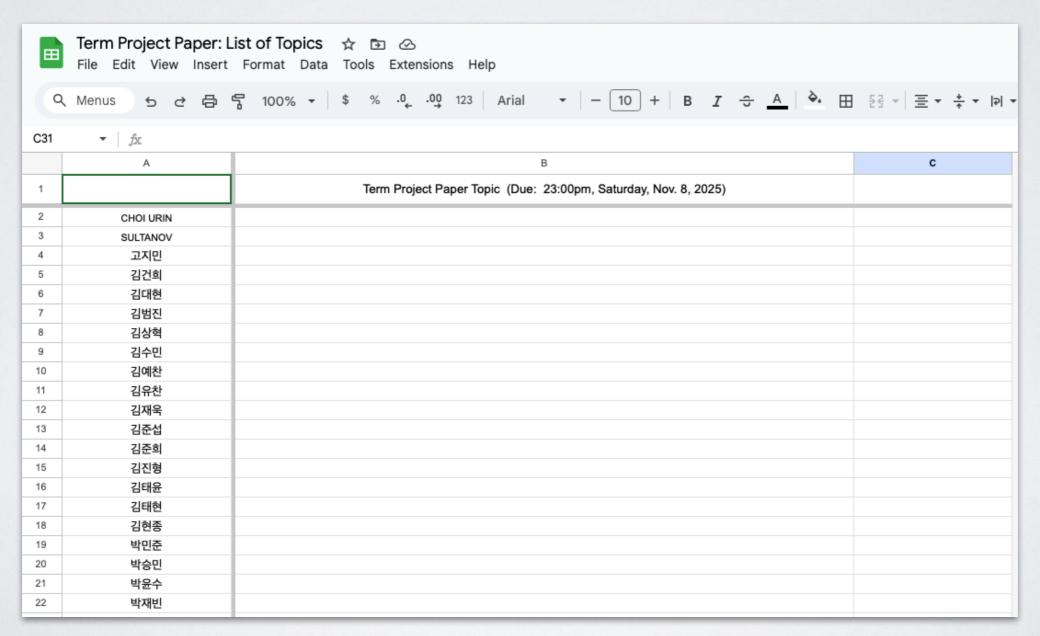
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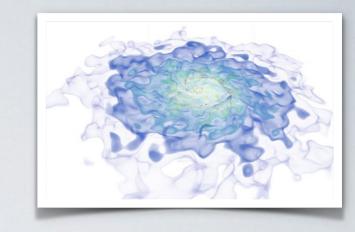


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 Post your topic by 23:00 pm, Nov. 8 (Sat) on a shared Google document below (expect late penalty of -0.5 pt/day):

https://docs.google.com/spreadsheets/d/117yyzo6Zp6dISAU5C7gyoNI03kjj8IM90b2MImP86yE

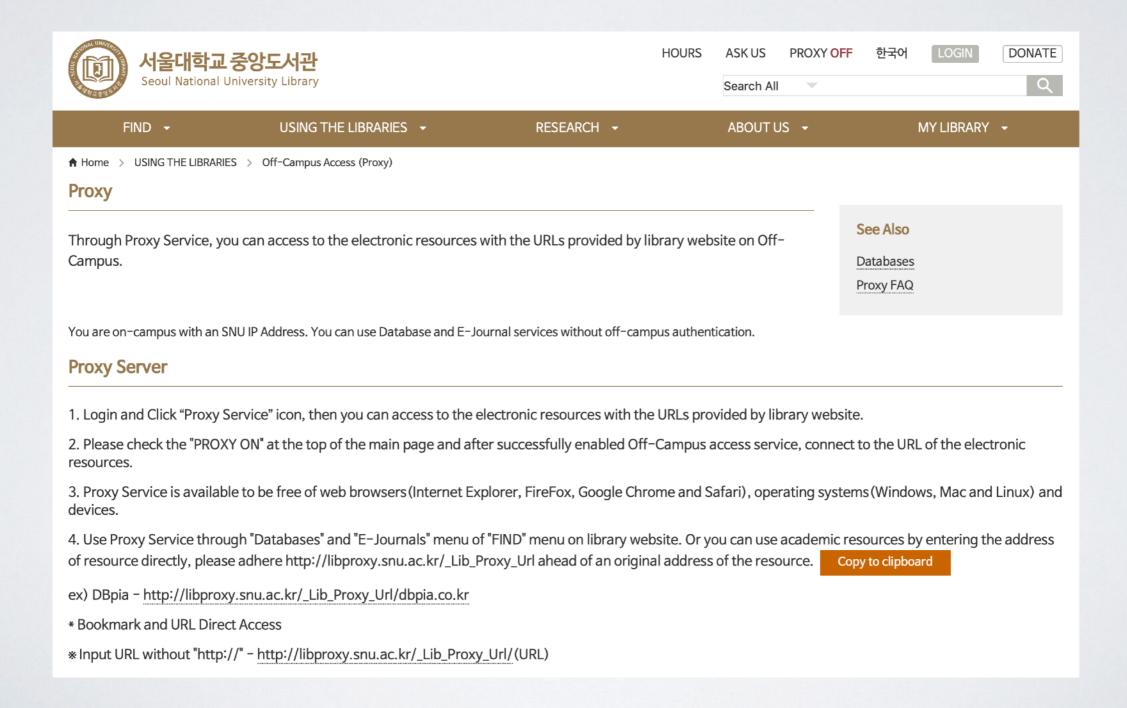




Quantity Doesn't Guarantee Quality!

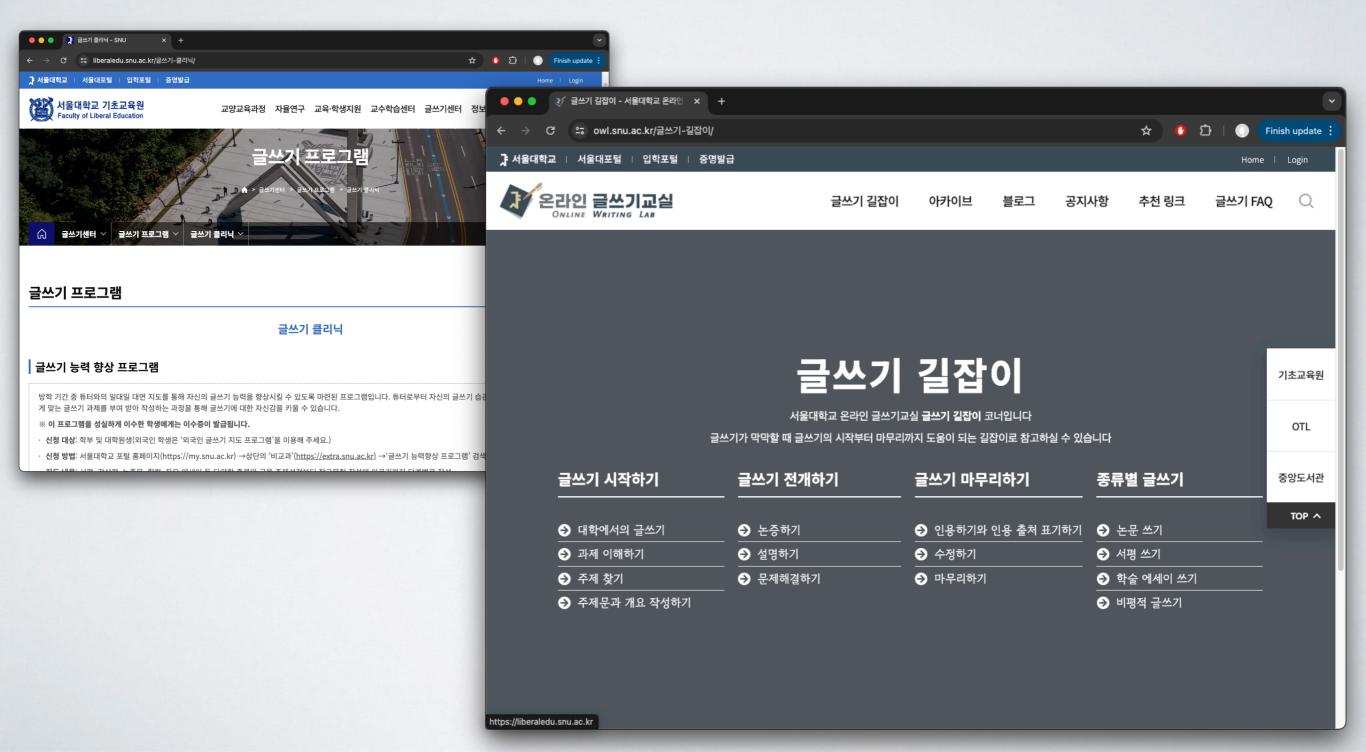
Electronic Resources via SNU Library

• To access e.g., academic journals off-campus via SNU library's proxy service, visit <u>library.snu.ac.kr/using/proxy</u>.

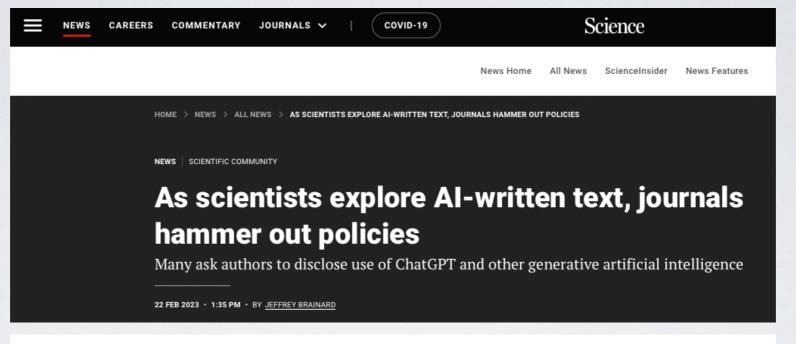


Resources via SNU Liberal Education

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Student Honor Code



SHARE:













One concern for journal managers is accuracy. If the software hasn't been exposed to enough training data to generate a correct response, it will often fabricate an answer, computer scientists have found. In November, Meta took down the public interface for Galactica, its scientist-specific large language model, just days after it was unveiled—users had identified myriad factual errors in the generated text. And a 2022 preprint study of Sparrow, an information-seeking chatbot developed by a Google subsidiary, found that up to 20% of its responses contained errors. AI text may also be biased toward established scientific ideas and hypotheses contained in the content on which the algorithms were trained. Journal editors also worry about ethics, suggesting authors who use text generators are sometimes presenting the outputs as if they wrote them—a transgression others have dubbed "aigiarism."

Many journals' new policies require that authors disclose use of text-generating tools and ban listing a large language model such as ChatGPT as a co-author, to underscore the human author's responsibility for ensuring the text's accuracy. That is the case for *Nature* and all Springer Nature journals, the JAMA Network, and groups that advise on best practices in publishing, such as the Committee on Publication Ethics and the World Association of Medical Editors. But at least one publisher has taken a tougher line: The *Science* family of journals announced a complete ban on generated text last month. The journals may loosen the policy in the future depending on what the scientific community decides is acceptable use of the text generators, Editor-in-Chief Holden Thorp says. "It's a lot easier to loosen our criteria than it is to tighten them."

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