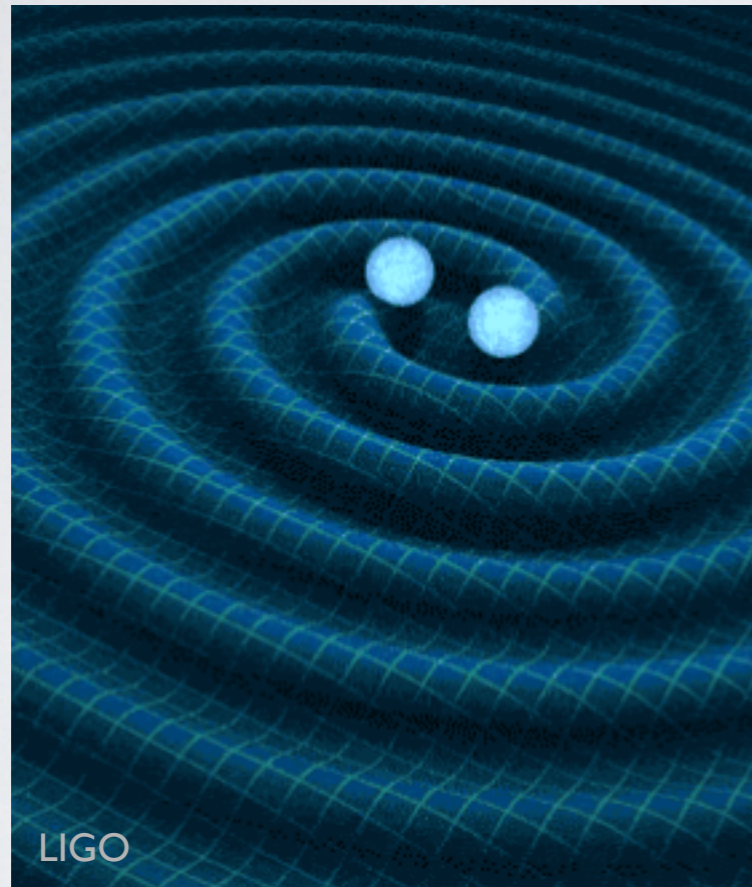


Week 3 - #2

Oscillations (III)



Today: Ch 3.8-3.9

Next Class: Ch 4.1-4.3

Ji-hoon Kim (Seoul National University)

Classical Mechanics I (Spring 2026): Quiz #5

— [open book and open note, **but** no cellphone or laptop, drop it off as you leave the class] —

Please write down your name and student ID in the top right corner. (0.0 pt: no paper found with your name / 0.5 pt: paper found with your name and some answers / 1.0 pt: good answers)

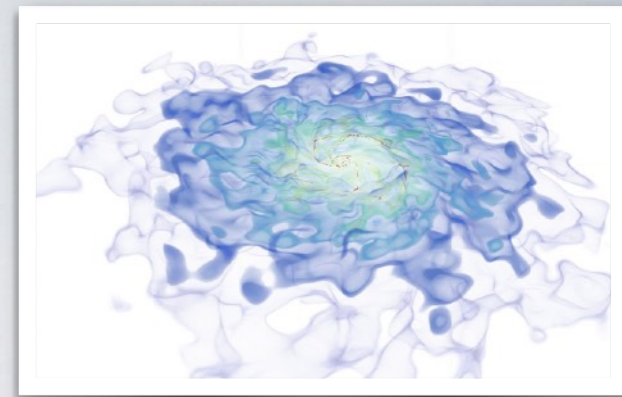
1. Thornton & Marion, Problem 3-11.
2. Thornton & Marion, Problem 3-28.



La Planète Affolée (1942)



Young Man Intrigued by the Flight of a Non-Euclidean Fly (1942, 1947)



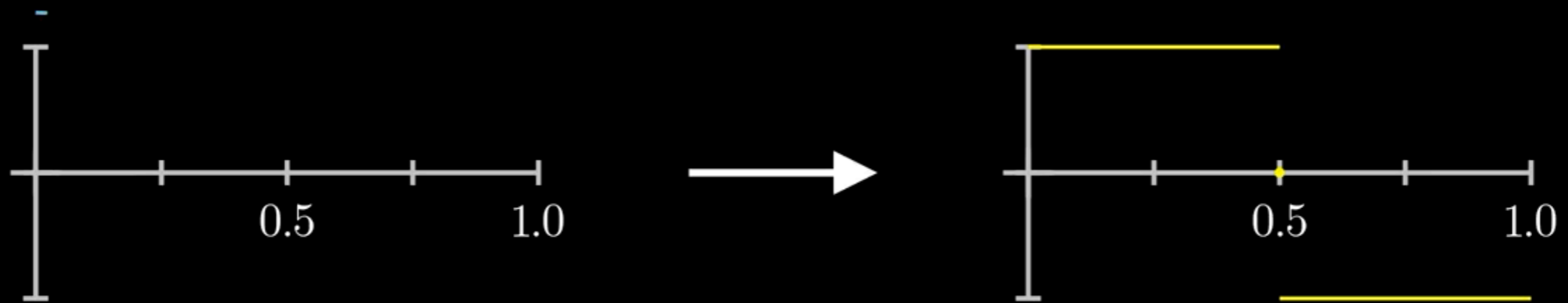
Sine-Cosine Fourier Series

Fourier Sine Series



Fourier Cosine Series

- A visualization of Fourier cosine series.



$$\frac{4}{\pi} \left(\frac{\cos(\pi x)}{1} - \frac{\cos(3\pi x)}{3} + \frac{\cos(5\pi x)}{5} - \dots \right) = \begin{cases} 1 & \text{if } x < 0.5 \\ 0 & \text{if } x = 0.5 \\ -1 & \text{if } x > 0.5 \end{cases}$$

For $0 \leq x \leq 1$

Sine-Cosine Fourier Series

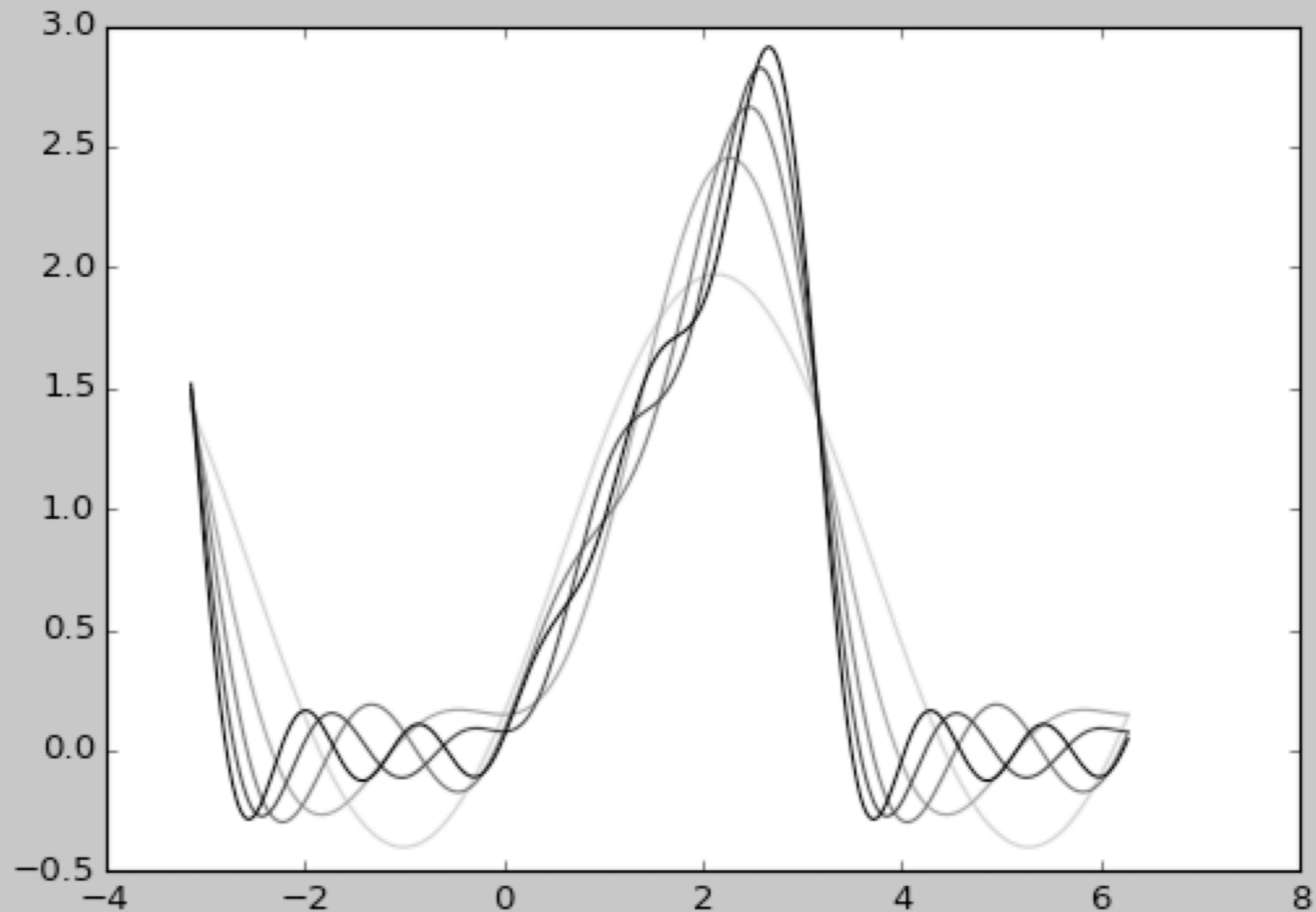
- A visualization of sine-cosine Fourier series (Ch 7.5, Prob 5.7).

```
import numpy as np
import matplotlib.pyplot as plt

N = 50 # partial sums up to the N-
t = np.arange(-np.pi, 2*np.pi, 0.6)

def my_fourier(n, t):
    partial_sum = [np.pi/4] * len(t)
    for nn in range(1, n+1):
        if nn%2==1:
            partial_sum += np.sin(
            partial_sum -= (2./np.
        else:
            partial_sum -= np.sin(
    return partial_sum

for n in range(N, N+1):
    col = 1. - float(n)/float(N)
    plt.plot(t, my_fourier(n, t),
plt.show()
```



Sine-Cosine Fourier Series

- A visualization of sine-cosine Fourier series (Ch 7.5, Prob 5.7).

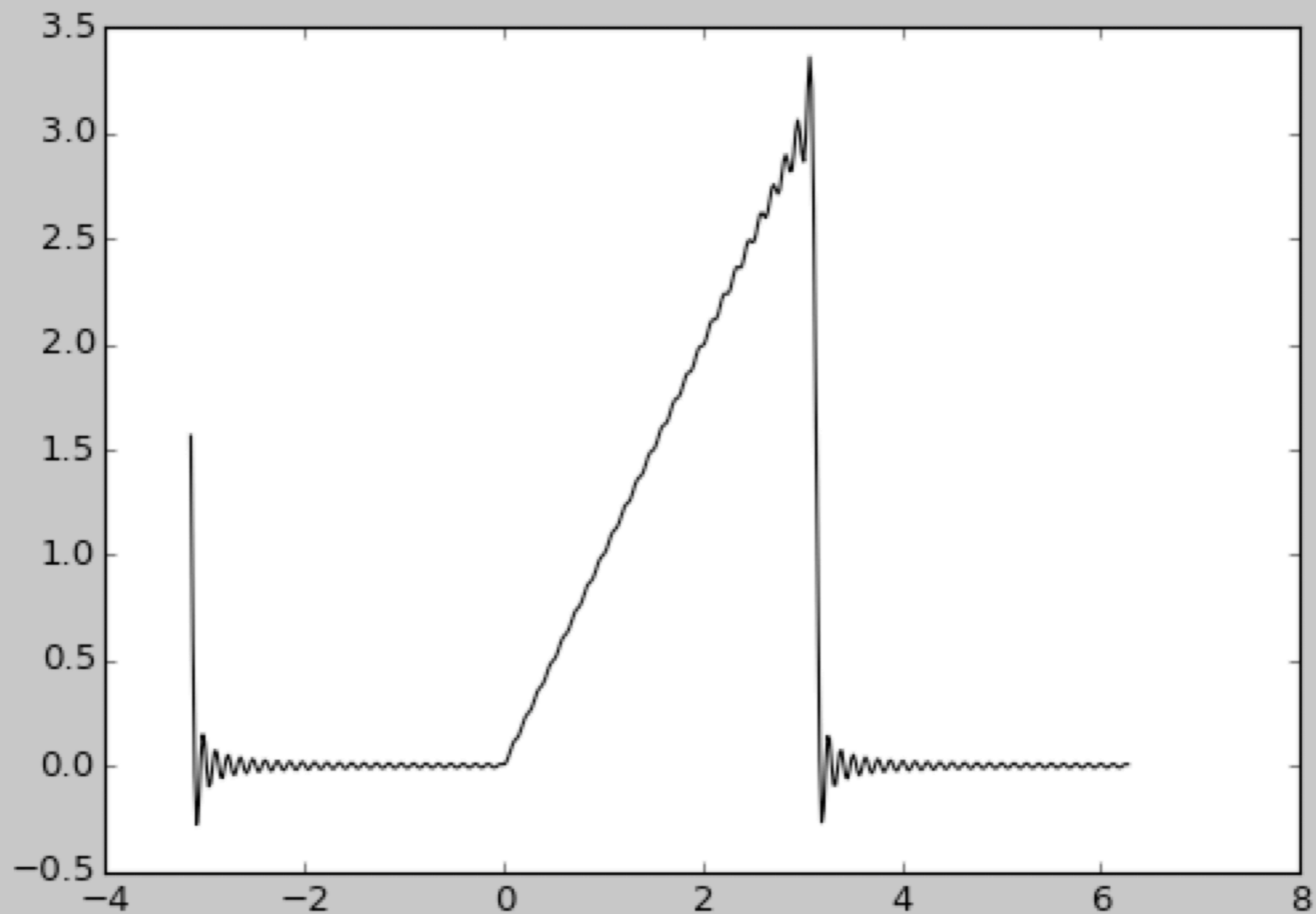
```
import numpy as np
import matplotlib.pyplot as plt

N = 50 # partial sums up to the N-
t = np.arange(-np.pi, 2*np.pi, 0.01)

def my_fourier(n, t):
    partial_sum = [np.pi/4] * len(t)
    for nn in range(1, n+1):
        if nn%2==1:
            partial_sum += np.sin(nn*t)
            partial_sum -= (2./np.pi) * np.cos(nn*t)
        else:
            partial_sum -= np.sin(nn*t)
            partial_sum += (2./np.pi) * np.cos(nn*t)
    return partial_sum

for n in range(N, N+1):
    col = 1. - float(n)/float(N)
    plt.plot(t, my_fourier(n, t), color=col)

plt.show()
```



Sine-Cosine Fourier Series

- A visualization of sine-cosine Fourier series (Ch 7.5, Prob 5.7).



$\pi/4 - (2/\pi) * [\cos(x) + \cos(3x)/3^2 + \cos(5x)/5^2] + [\sin(x) - \sin(2x) / 2 + \sin(3x)/3 - \sin(4x)/4 + \sin(5$

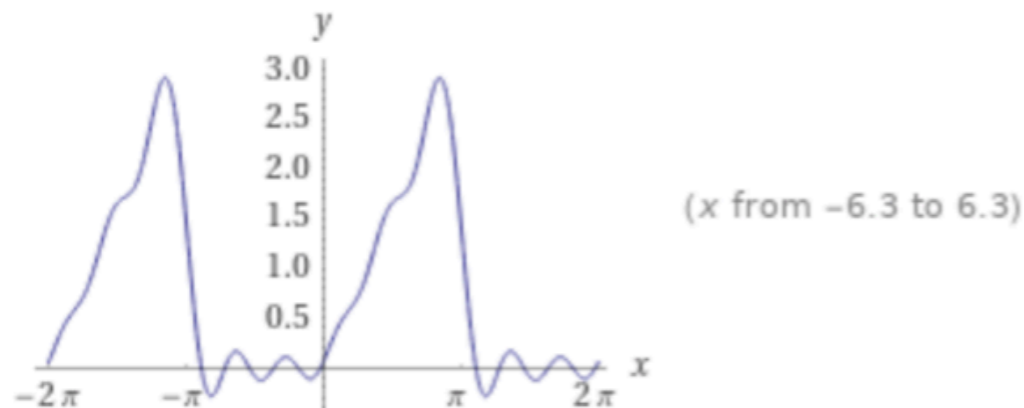
NATURAL LANGUAGE MATH INPUT

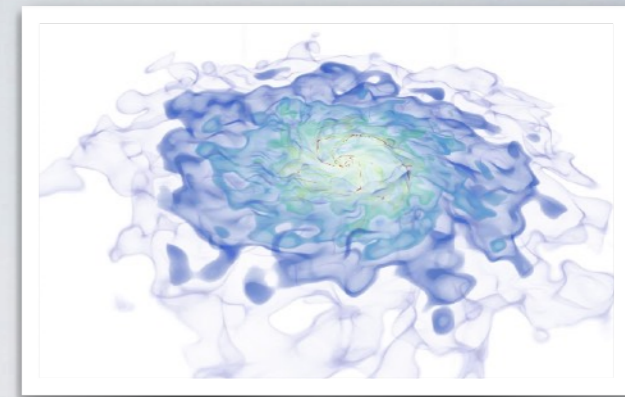
EXTENDED KEYBOARD EXAMPLES UPLOAD RANDOM

Input

$$\frac{\pi}{4} - \frac{2}{\pi} \left(\cos(x) + \frac{\cos(3x)}{3^2} + \frac{\cos(5x)}{5^2} \right) + \left(\sin(x) - \frac{1}{2} \sin(2x) + \frac{1}{3} \sin(3x) - \frac{1}{4} \sin(4x) + \frac{1}{5} \sin(5x) \right)$$

Plots

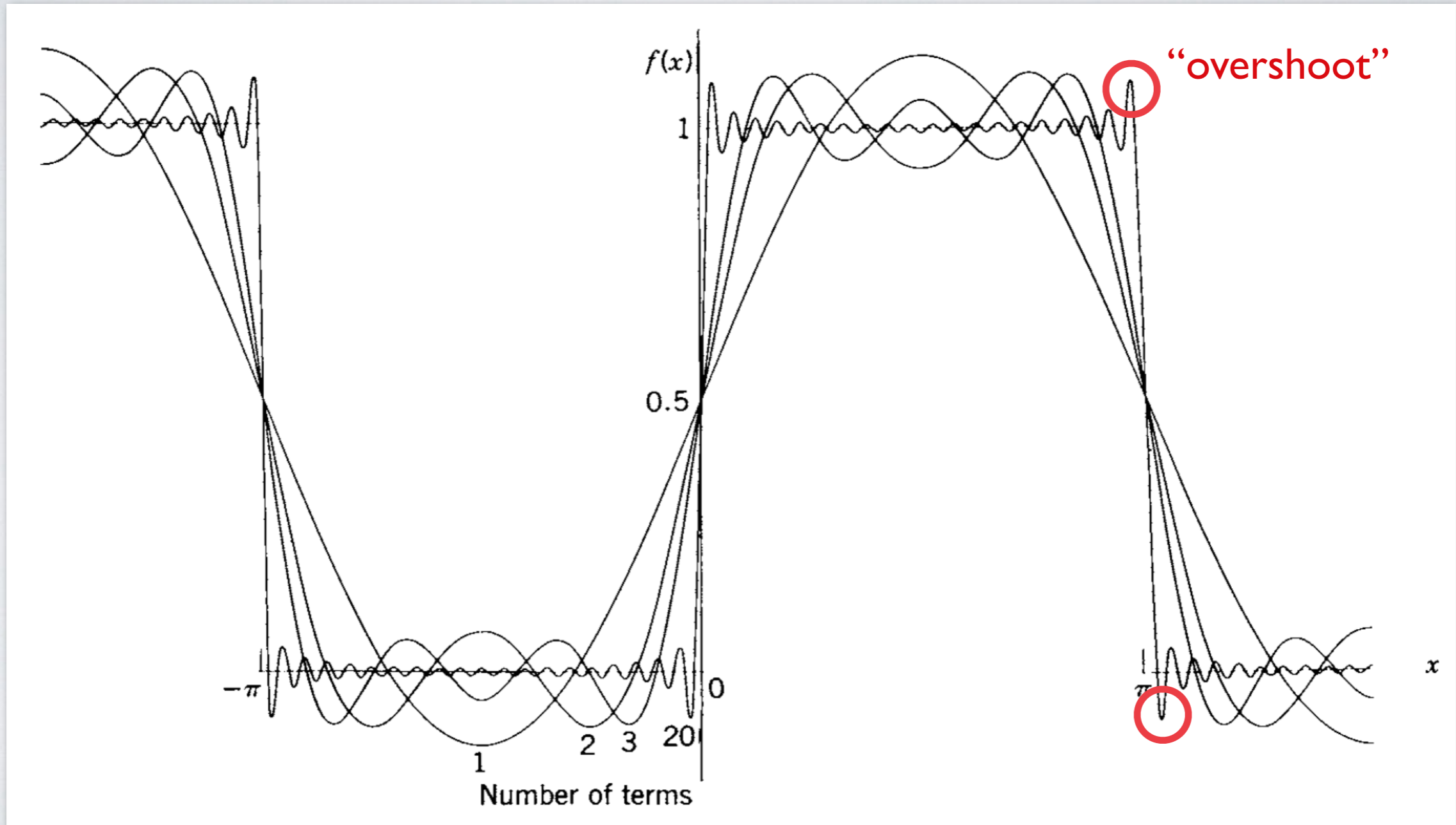




Gibbs Phenomenon

Fourier Sine Series

- A visualization of Fourier sine series (Ch 7.6, Figure 6.2).



Sine-Cosine Fourier Series

- A visualization of sine-cosine Fourier series (Ch 7.5, Prob 5.7).

```
import numpy as np
import matplotlib.pyplot as plt

N = 50 # partial sums up to the N-
t = np.arange(-np.pi, 2*np.pi, 0.01)

def my_fourier(n, t):
    partial_sum = [np.pi/4] * len(t)
    for nn in range(1, n+1):
        if nn%2==1:
            partial_sum += np.sin(nn*t)
            partial_sum -= (2./np.pi) * np.cos(nn*t)
        else:
            partial_sum -= np.sin(nn*t)
            partial_sum += (2./np.pi) * np.cos(nn*t)
    return partial_sum

for n in range(N, N+1):
    col = 1. - float(n)/float(N)
    plt.plot(t, my_fourier(n, t), col)

plt.show()
```

