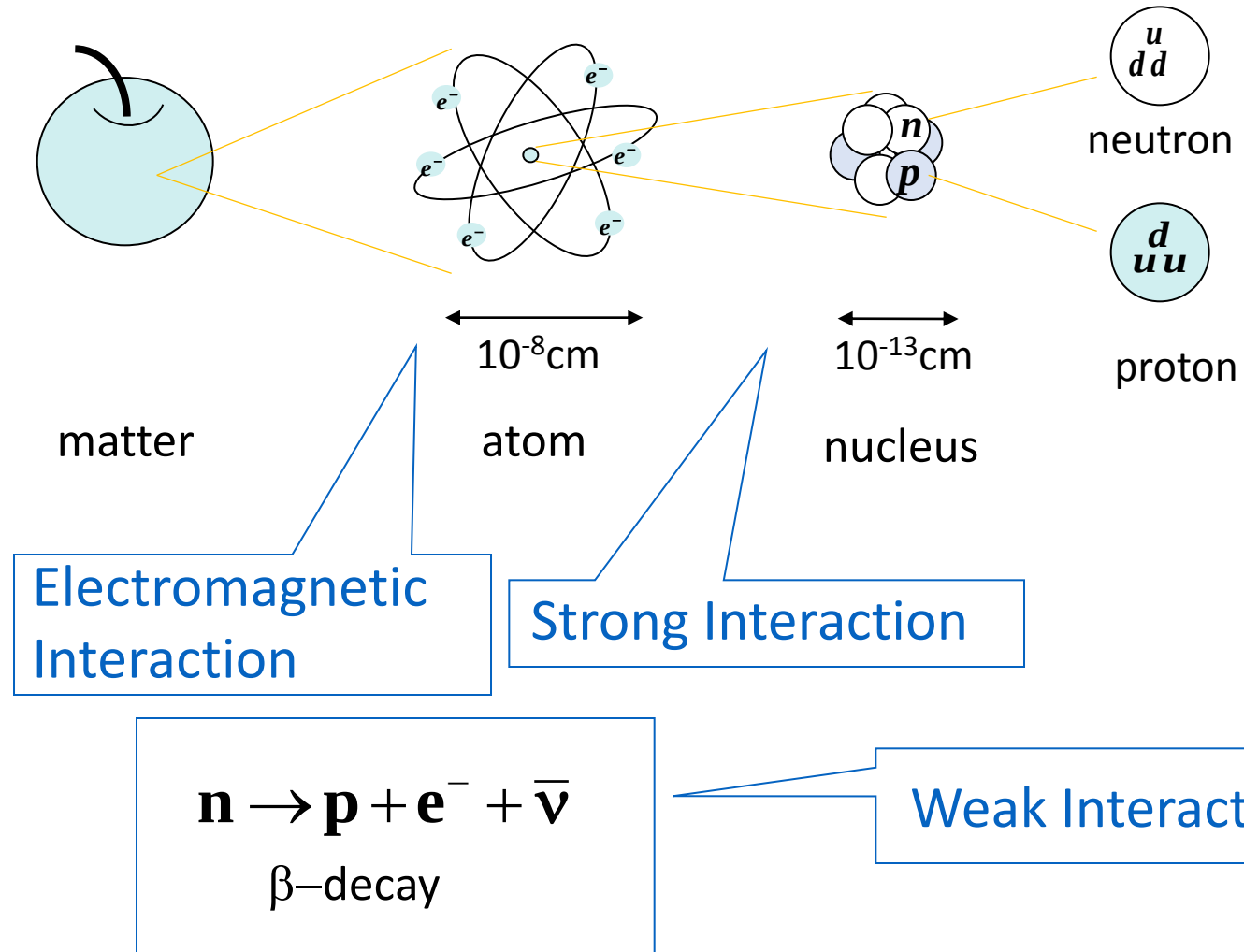


2015/10/08
Seoul Univ.

Matter and Antimatter

KEK and JSPS
M. Kobayashi

Structure of matter



Discovery of Antiparticle

Special Relativity (1905)

Quantum Mechanics (1925)

Schrodinger equation

$$i\hbar \frac{\partial}{\partial t} \psi(\mathbf{x}) = -\frac{\hbar^2}{2m} \frac{\partial^2}{\partial \mathbf{x}^2} \psi(\mathbf{x})$$

$$\leftarrow E = \frac{p^2}{2m}$$



Dirac equation (Dirac 1928)

$$i\hbar \frac{\partial}{\partial t} \psi(\mathbf{x}) = \left(\frac{\hbar c}{i} \vec{\alpha} \cdot \frac{\partial}{\partial \vec{\mathbf{x}}} + \beta mc^2 \right) \psi(\mathbf{x})$$

$\vec{\alpha}, \beta : 4 \times 4 \text{ matrix}$

$$\psi = \begin{pmatrix} \psi_1 \\ \psi_2 \\ \psi_3 \\ \psi_4 \end{pmatrix}$$

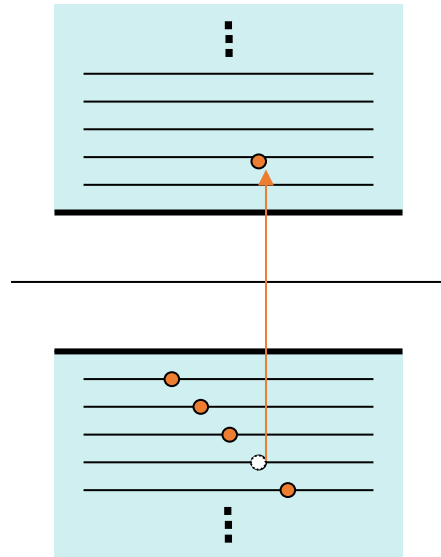
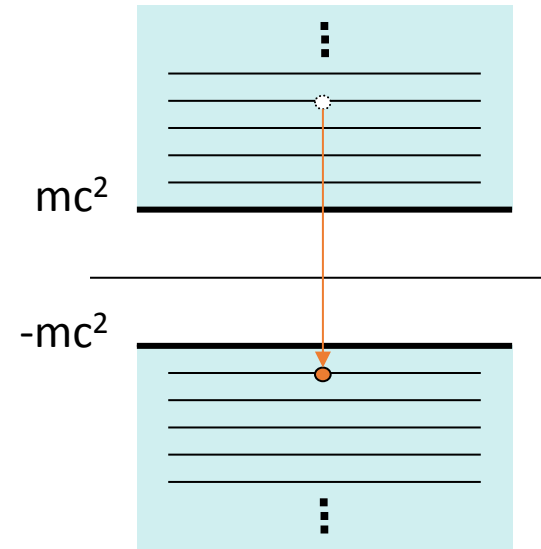
Solutions of the Dirac equation

Positive energy

$$E = \sqrt{\mathbf{p}^2 c^2 + m^2 c^4} \geq mc^2$$

Negative energy

$$E = -\sqrt{\mathbf{p}^2 c^2 + m^2 c^4} \leq -mc^2$$



Dirac Sea

All negative energy states are occupied

Hole in the Dirac Sea



Positively charged particle

1932 Anderson Discovery of Positron

Dirac's arguments: only for fermions

How about bosons ?



Relativistic Quantum Field Theory

Every particle has its corresponding antiparticle

- same mass
- opposite charge

Note

- Self conjugate particle: a particle and an antiparticle are identical

Example: Photon

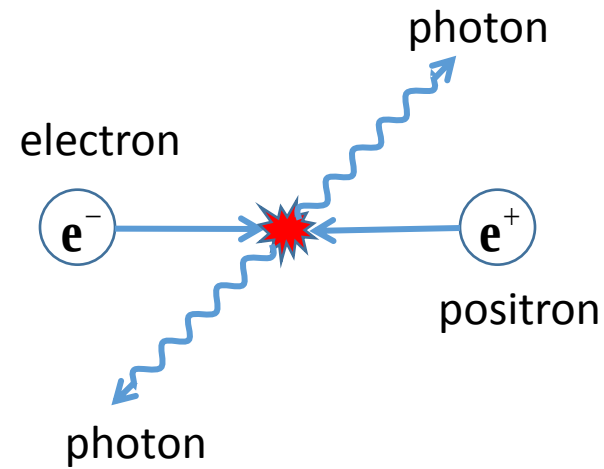
- Neutral particles are not necessarily self conjugate

Example: Neutron

electron e^- $\Leftrightarrow$ positron e^+
proton p $\Leftrightarrow$ antiproton $\bar{p}$
neutron n $\Leftrightarrow$ antineutron $\bar{n}$

Pair annihilation

$$e^- + e^+ \rightarrow \gamma + \gamma$$



Pair annihilation

$$e^{-} + e^{+} \rightarrow \gamma + \gamma$$

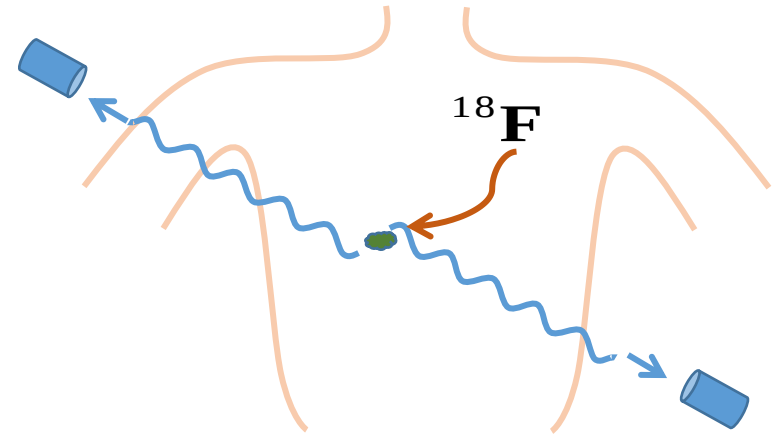
$$p + \bar{p} \rightarrow \pi + \pi + \dots$$

Pair creation

$$\gamma + \gamma \rightarrow e^{+} + e^{-}$$

$$p + p \rightarrow p + p + p + \bar{p}$$

PET



CP symmetry

Invariance of the laws of nature under the exchange of particle and antiparticle

C (charge conjugation) : simple exchange of particle and antiparticle

P (parity) : space inversion

CP : combined operation of C and P

P violation was found in 1956.

→ C is also violated, but CP looked to hold true

Discovery of CP violation

1964 Cronin, Fitch et al

~0.2% of K_L decay into

$$\mathbf{K}_L \rightarrow \pi^+ + \pi^-$$

$$|\mathbf{K}_L\rangle = \mathbf{p} |\mathbf{K}^0\rangle + \mathbf{q} |\bar{\mathbf{K}}^0\rangle$$

$$|\mathbf{p}| \neq |\mathbf{q}| \Rightarrow \mathbf{CP\ violation}$$

Hadron : strongly interaction particles

proton p

neutron n

pion $\pi^+ \pi^- \pi^0$

kaon $K^+ K^- K^0 \bar{K}^0$

lambda Λ

sigma $\Sigma^+ \Sigma^- \Sigma^0$

1956 Sakata Sakata Model

All the hadrons are composite states of

p, n, Λ

: Fundamental Triplet

$p\bar{n}$

π^+

$p\bar{\Lambda}$

K^+

$\Lambda p\bar{n}$

Σ^+

$\Lambda\Lambda\bar{n}$

Ξ^0

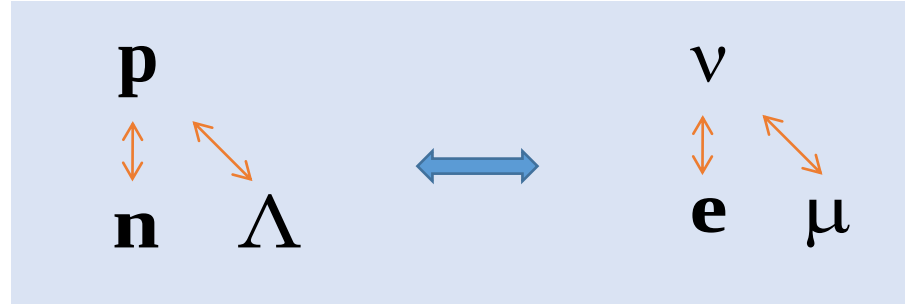


Courtesy of Sakata Memorial
Archival Library

Shoichi Sakata

1911-1970

Weak Interaction in the Sakata Model



1959 Gamba, Marshak, Okubo
B-L Symmetry

1960 Maki, Nakagawa, Ohnuki, Sakata

Nagoya Model : $\mathbf{p} = \langle \mathbf{B}^+ \nu \rangle$, $\mathbf{n} = \langle \mathbf{B}^+ e \rangle$, $\Lambda = \langle \mathbf{B}^+ \mu \rangle$

$\mathbf{B}^+$: B-matter

Discovery of Two Neutrinos

1962 Danby et al. PRL 9, 36 (1962)

$$\begin{array}{cc} \nu_e & \nu_\mu \\ \updownarrow & \updownarrow \\ e & \mu \end{array}$$

Modification of Nagoya Model

1962 Katayama, Matumoto, Tanaka and Yamada
Progr. Theor. Phys. 28, 675 (1962)

1962 Maki, Nakagawa and Sakata
Progr. Theor. Phys. 28, 870 (1962)

$$\mathbf{p} = \langle \mathbf{B}^+ \nu_1 \rangle, \quad \mathbf{n} = \langle \mathbf{B}^+ e \rangle, \quad \Lambda = \langle \mathbf{B}^+ \mu \rangle, \quad \mathbf{p}' = \langle \mathbf{B}^+ \nu_2 \rangle$$

$$\nu_1 = \cos \delta \nu_e + \sin \delta \nu_\mu$$

$$\nu_2 = -\sin \delta \nu_e + \cos \delta \nu_\mu$$

Neutrino Mixing: Maki, Nakagawa, Sakata (MNS)

$$\mathbf{p} = \langle \mathbf{B}^+ \mathbf{v}_1 \rangle, \quad \mathbf{n} = \langle \mathbf{B}^+ \mathbf{e} \rangle, \quad \Lambda = \langle \mathbf{B}^+ \mu \rangle, \quad \mathbf{p}' = \langle \mathbf{B}^+ \mathbf{v}_2 \rangle$$

$$\mathbf{v}_1 = \cos \delta \mathbf{v}_e + \sin \delta \mathbf{v}_\mu$$

$$\mathbf{v}_2 = -\sin \delta \mathbf{v}_e + \cos \delta \mathbf{v}_\mu$$

Identify $\mathbf{v}_1, \mathbf{v}_2$ as the mass eigenstates

$$\begin{array}{cc} \nu_e & \nu_\mu \\ \updownarrow & \updownarrow \\ e & \mu \end{array}$$

They formulated lepton flavor mixing precisely.

$$\text{Bare field: } \psi_0 = \begin{pmatrix} \mu_0 \\ \mathbf{e}_0 \end{pmatrix}, \quad \varphi_0 = \begin{pmatrix} \nu_{\mu 0} \\ \nu_{e 0} \end{pmatrix}$$

$$\mathbf{L}_{\text{int}} = [(\bar{\psi}_0 \Lambda \psi_0) + (\bar{\varphi}_0 \Lambda' \varphi_0)] \mathbf{X}^* \mathbf{X}$$

Λ, Λ' : 2x2 mass matrices

Difference of mass diagonalization



Mixing angle



S. Sakata

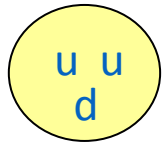
Z. Maki

M. Nakagawa

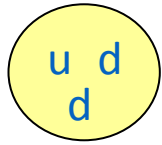
Quark Model

1964 Gell-Mann

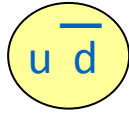
quark u d s
 $2/3e$ $-1/3e$ $-1/3e$



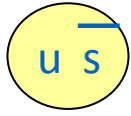
proton



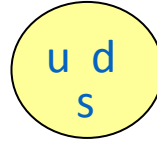
neutron



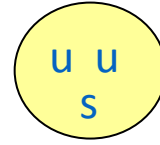
π^+



K^+



Λ



Σ^+

1963 Cabibbo

Cabibbo angle θ_c

$$u \leftrightarrow d' = \cos \theta_c d + \sin \theta_c s$$

Status at the end of 1960's

Fundamental particles

quarks	u	
	d	s
leptons	ν_e	ν_μ
	e	μ

Fundamental interactions

Electromagnetic	Renormalization theory
	Tomonaga-Schwinger-Feynman
Weak	No satisfactory theory
Strong	

1971 't Hooft : Renormalization of Non-Abelian gauge theory

-
- Weinberg-Salam-Glashow theory for Electro-Weak Int.
 - QCD for Strong Int.

1973 Kobayashi, Maskawa

How to accommodate CP violation

What we found

- Not possible with three or four quarks
- Existence of unknown particles
- A possible candidate is six-quark model

u	c	t
d	s	b

Flavor Mixing of 4-Quark Model

$$\begin{pmatrix} u \\ d' \end{pmatrix}_L \quad \begin{pmatrix} c \\ s' \end{pmatrix}_L \quad \begin{pmatrix} d' \\ s' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} \\ V_{cd} & V_{cs} \end{pmatrix} \begin{pmatrix} d \\ s \end{pmatrix}$$

Redefinition of quark fields

$$u \rightarrow e^{i\delta_u} u, \quad d \rightarrow e^{i\delta_d} d, \dots$$

$$\begin{pmatrix} e^{-i\delta_u} & 0 \\ 0 & e^{-i\delta_c} \end{pmatrix} \begin{pmatrix} V_{ud} & V_{us} \\ V_{cd} & V_{cs} \end{pmatrix} \begin{pmatrix} e^{i\delta_d} & 0 \\ 0 & e^{i\delta_s} \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$$



No CP Violation

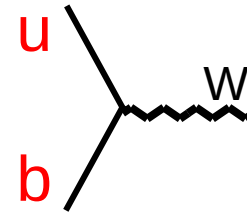
6-Quark Model for CP Violation

$$\begin{pmatrix} u \\ d' \end{pmatrix} \quad \begin{pmatrix} c \\ s' \end{pmatrix} \quad \begin{pmatrix} t \\ b' \end{pmatrix} \quad \begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \approx \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

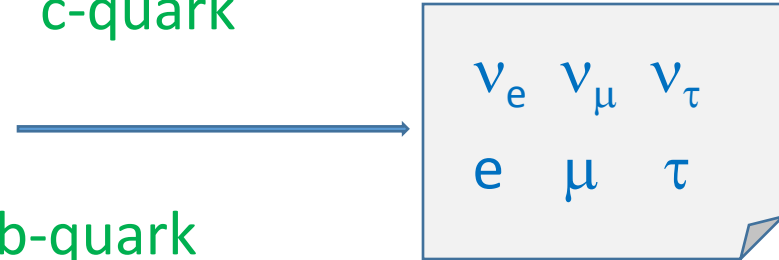


Complex Coupling Constant



Development of Experiments

- 1974 Discovery of J/ψ particle c-quark
- 1975 Discovery of τ -lepton
- 1977 Discovery of Y particle b-quark
- 1995 Discovery of t-quark



Theory of Strong Interactions

- 1973 QCD Asymptotic freedom
 → Quark confinement



Standard Model

Status at the end of 1960's

Fundamental particles

quarks	u	c	t
	d	s	b
leptons	ν_e	ν_μ	ν_τ
	e	μ	τ

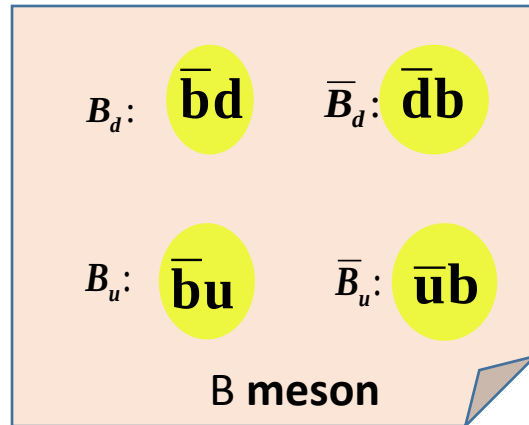
Fundamental interactions

Electromagnetic	}	Renormalization theory
Weak		Tomonaga-Schwinger-Feynman
Strong	}	Weinberg-Salam-Glashow Theory
		No satisfactory theory
		QCD

CP violation experiments at B-factories

B-factories at KEK and SLAC

- e^+e^- collider
- optimized for B-meson production
- asymmetric energy





KEKB/Belle (Japan)

$E(e^-)=8\text{GeV}$,
 $E(e^+)=3.5\text{GeV}$
Finite angle beam crossing

1994

May 1999 –
Jun. 2010



Super KEBB



PEP-II/BaBar (US)

$E(e^-)=9\text{GeV}$,
 $E(e^+)=3.1\text{GeV}$
Zero angle beam crossing

1993

May 1999 –
Apr. 2008

Feature

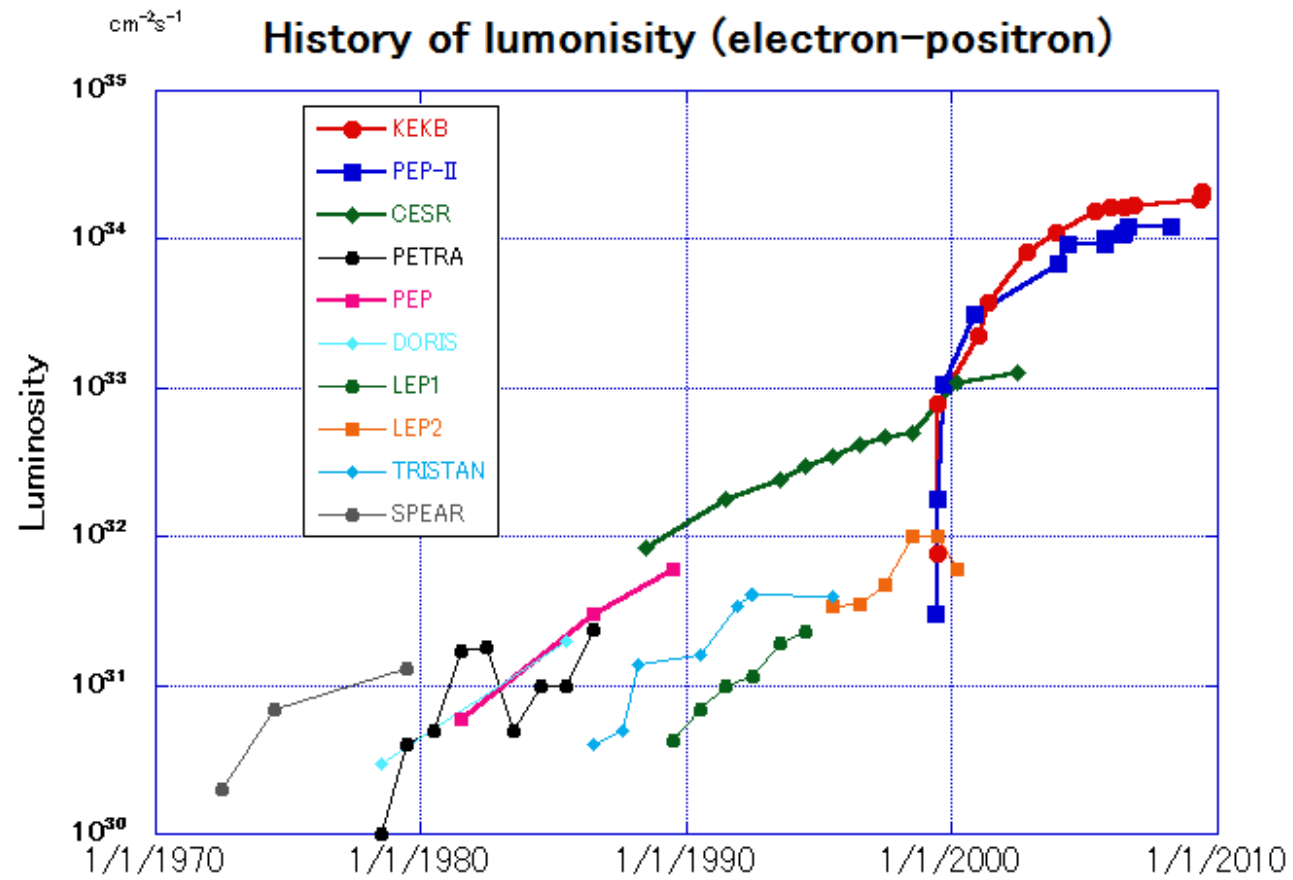
Governmental
Approval

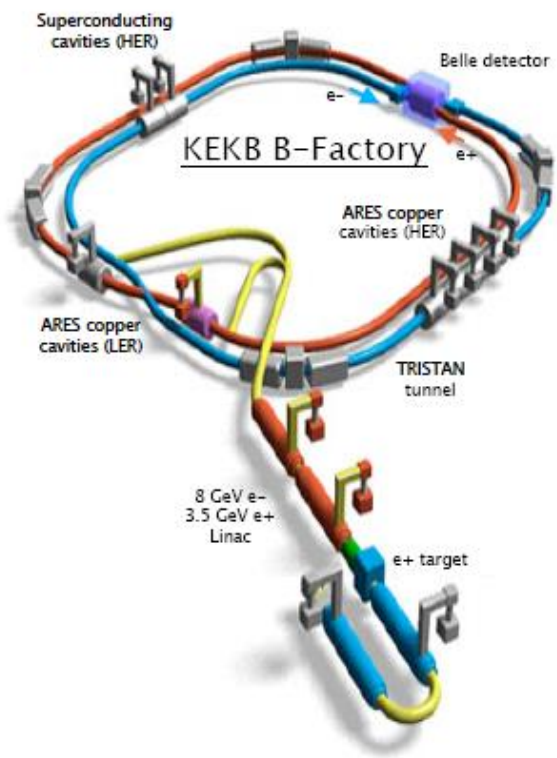


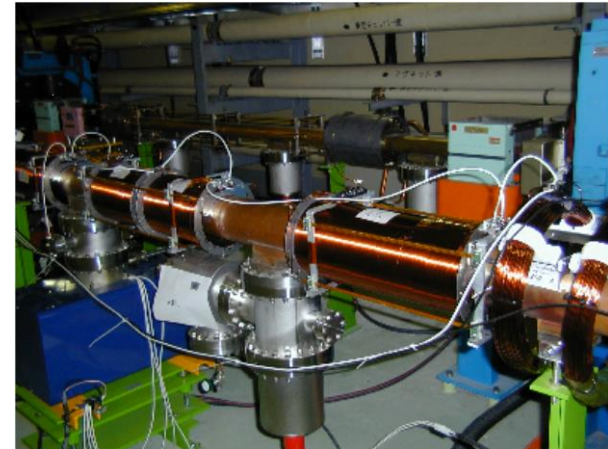
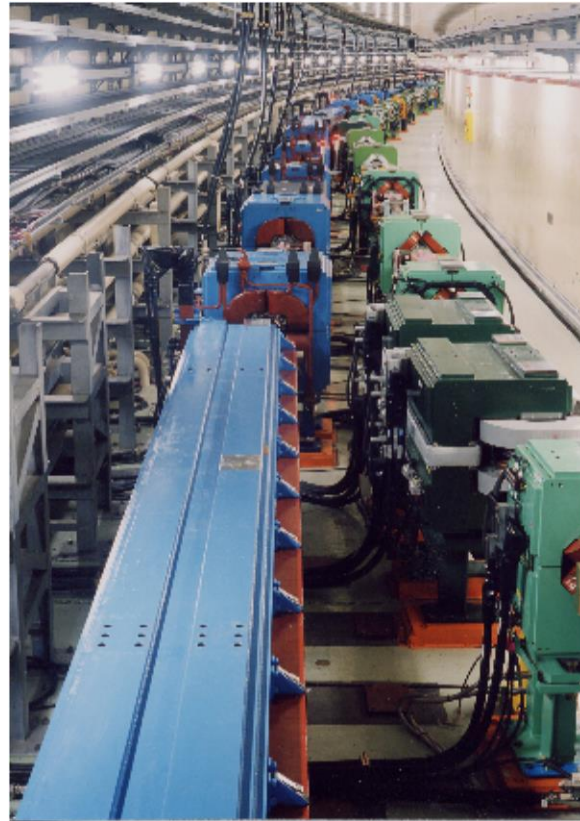
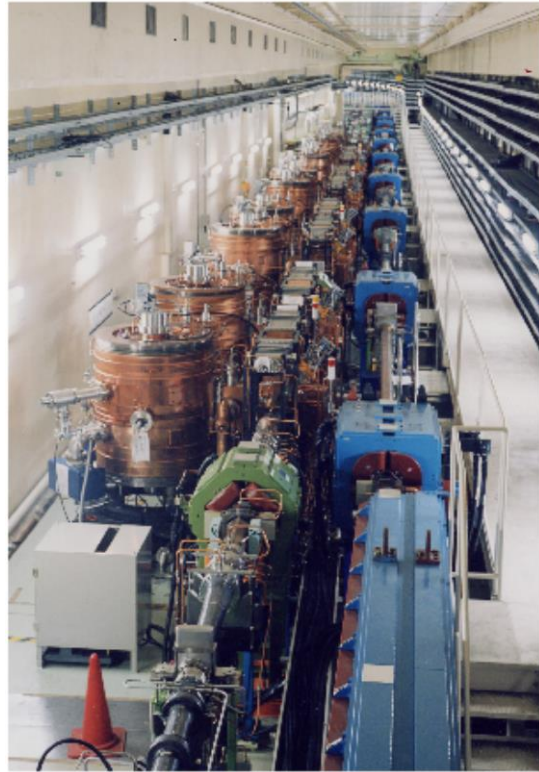
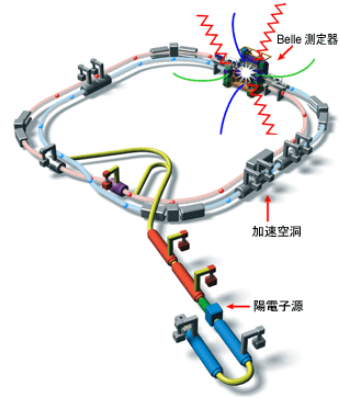
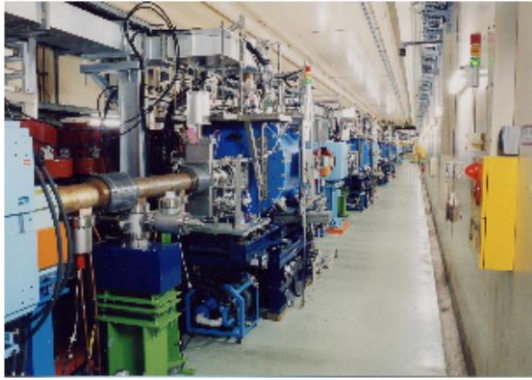
Experiment

$$\text{KEKB } L = 2.1 \times 10^{34} \text{ cm}^{-2} \text{ sec}^{-1}$$

$$\text{PEP-II } L = 1.2 \times 10^{34} \text{ cm}^{-2} \text{ sec}^{-1}$$

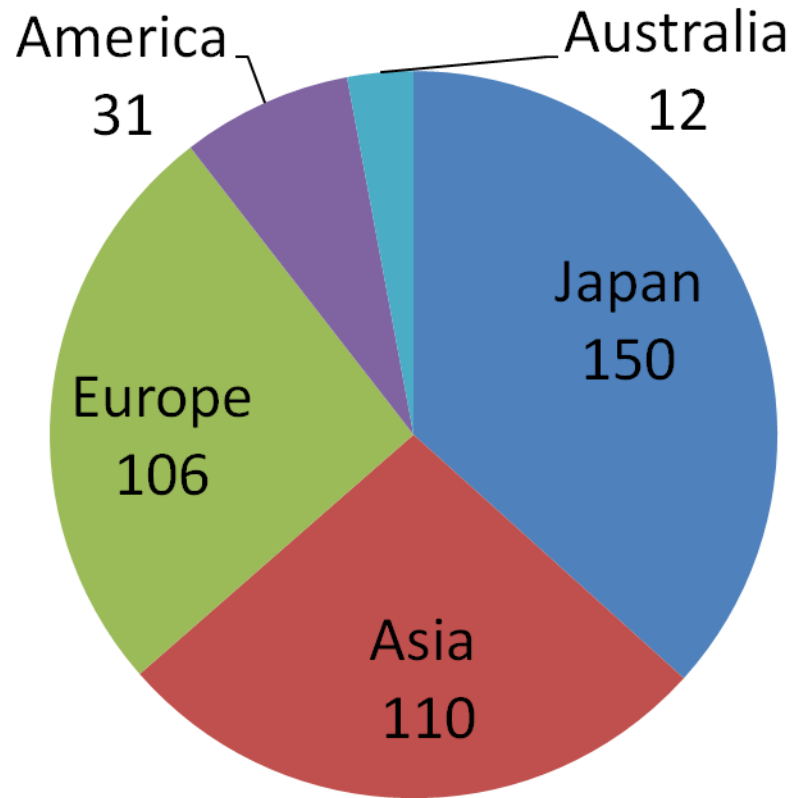


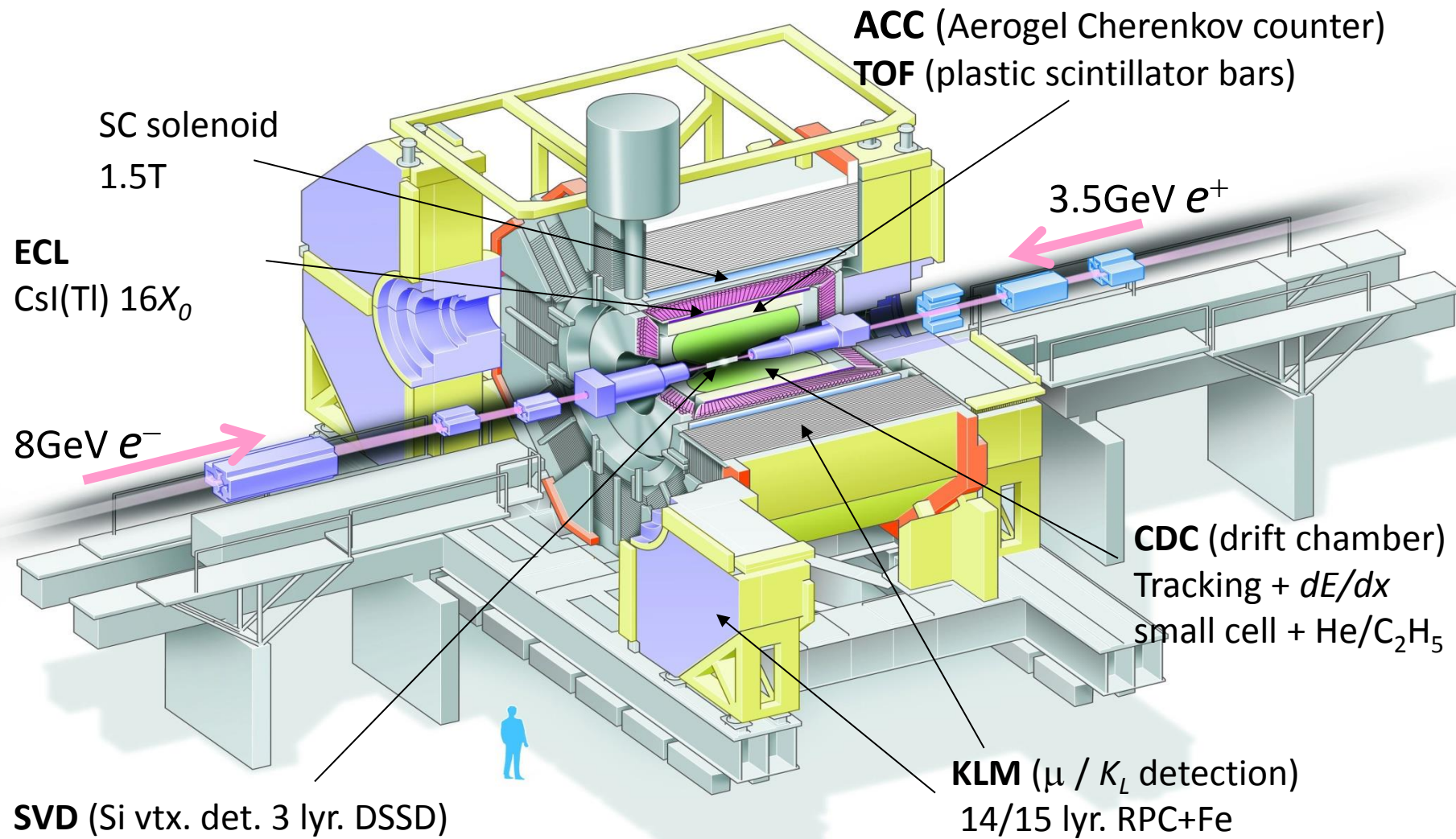


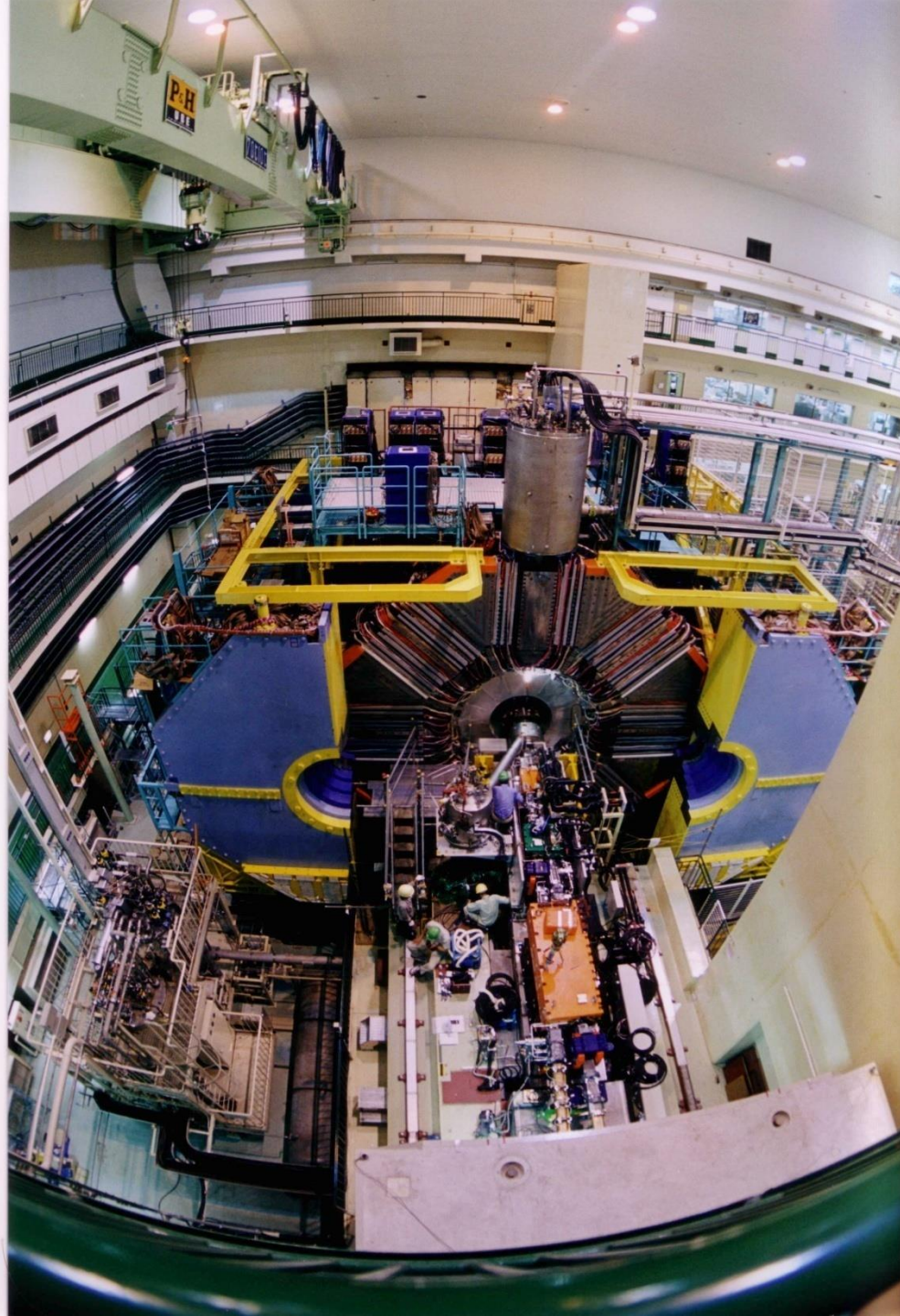


Belle Members

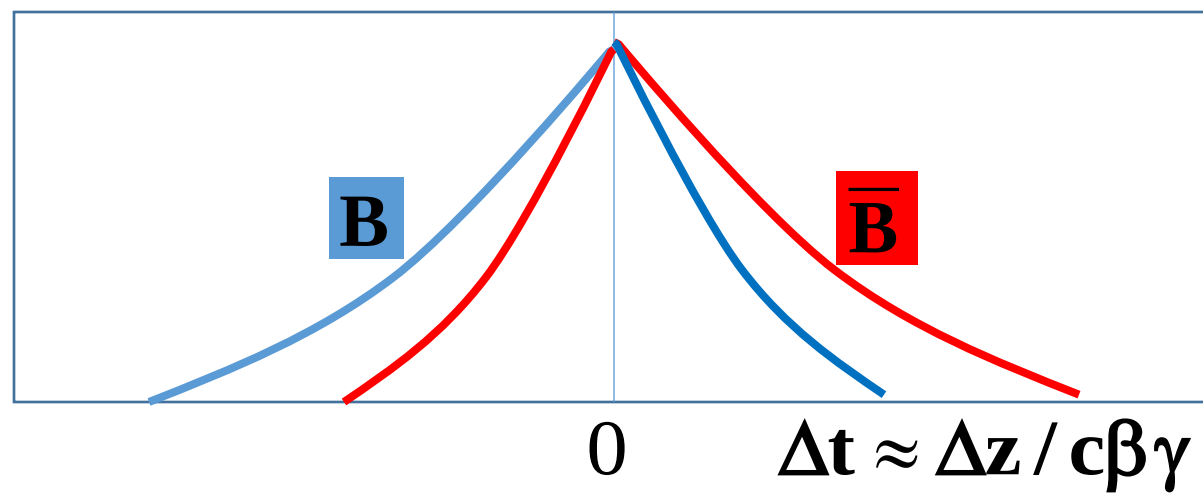
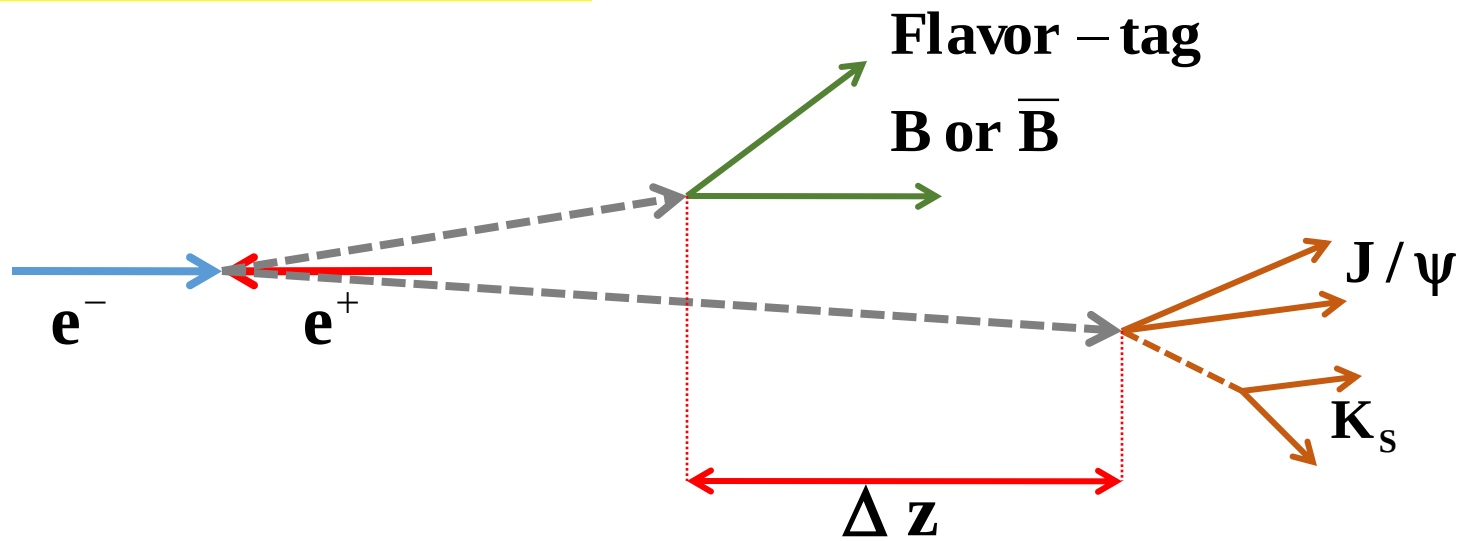
15 Countries and Regions
62 Institution
409 Members







$$e^+ + e^- \rightarrow B_d + \bar{B}_d$$



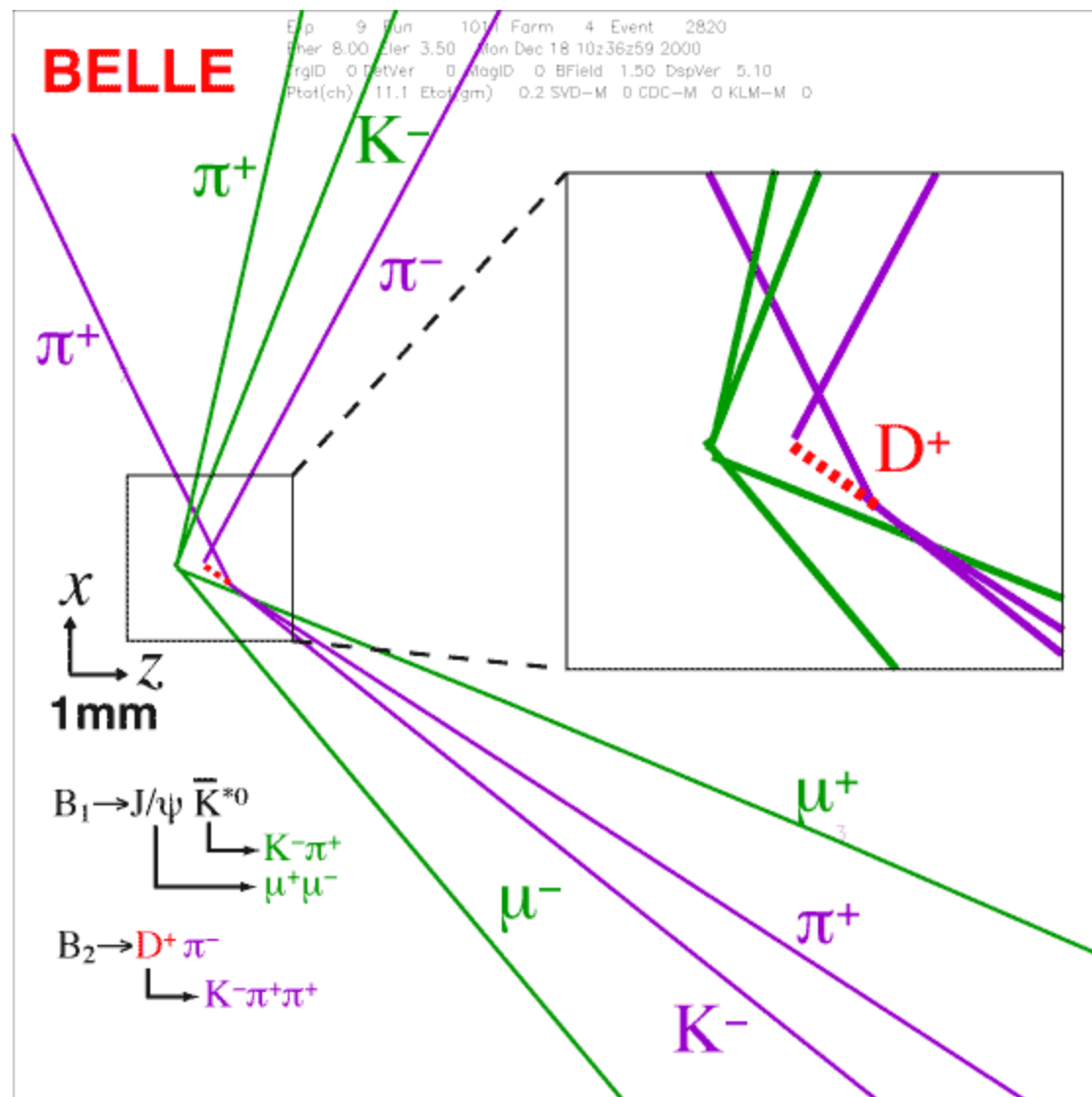
BELLE

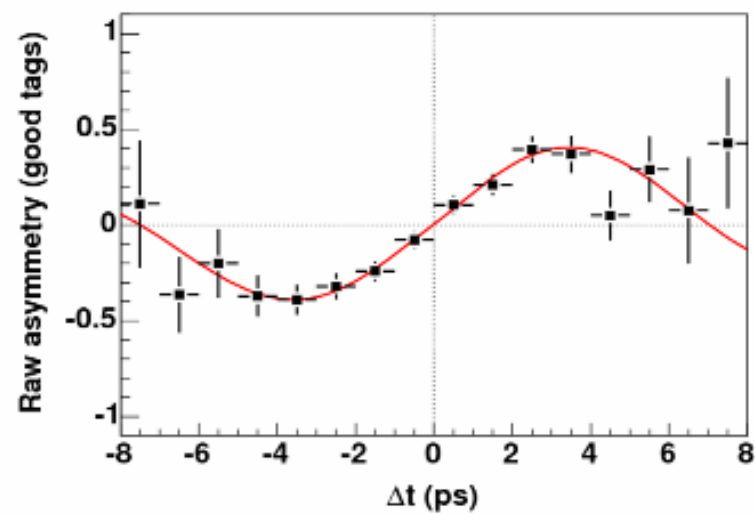
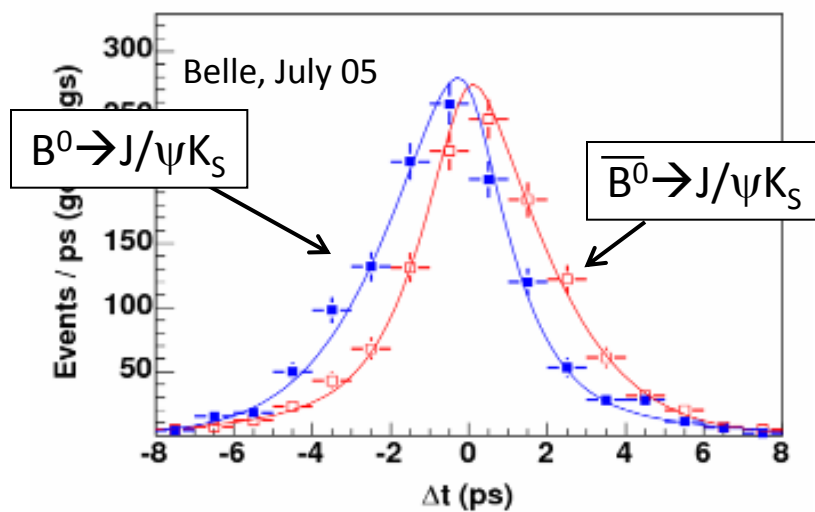
Exp 9 Run 1011 Farm 4 Event 2820
Eher 8.00 Eler 3.50 Mon Dec 18 10:36:59 2000
TrglD 0 DelVer 0 MagID 0 BField 1.50 DspVer 5.10
Plot(ch) 11.1 Etot(gm) 0.2 SVD-M 0 CDC-M 1 KLM-M 0

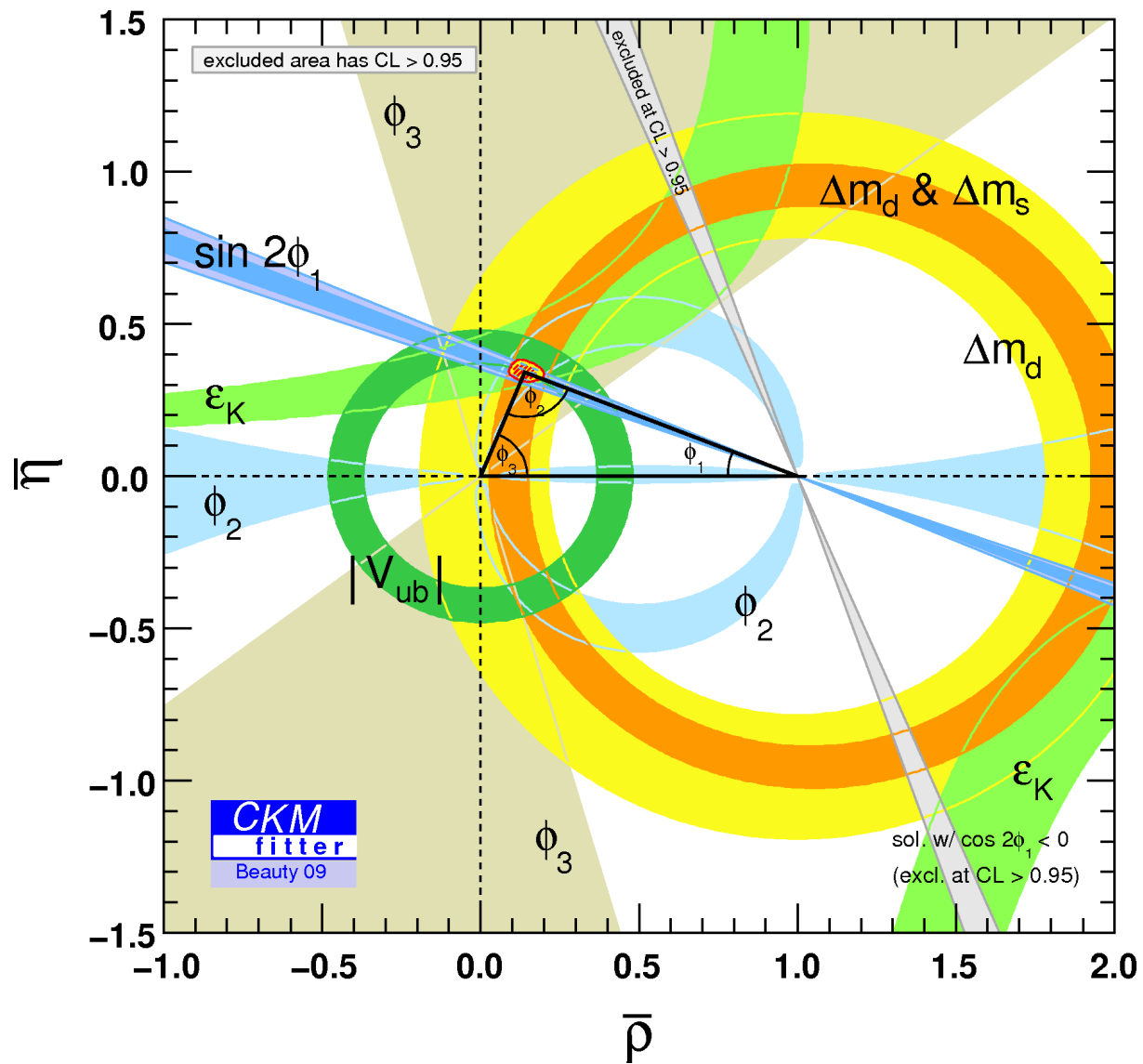
$B_1 \rightarrow J/\psi \bar{K}^{*0}$
 $\quad \quad \quad \swarrow \searrow$
 $\quad \quad \quad K^- \pi^+$
 $\quad \quad \quad \mu^+ \mu^-$

$B_2 \rightarrow D^+ \pi^-$
 $\quad \quad \quad \swarrow$
 $\quad \quad \quad K^- \pi^+ \pi^+$

20 cm



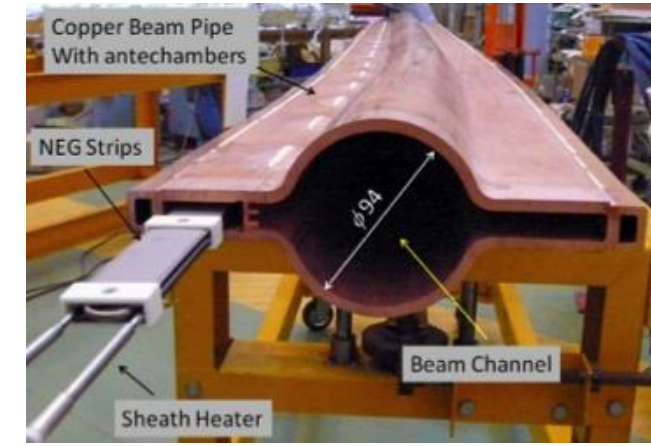
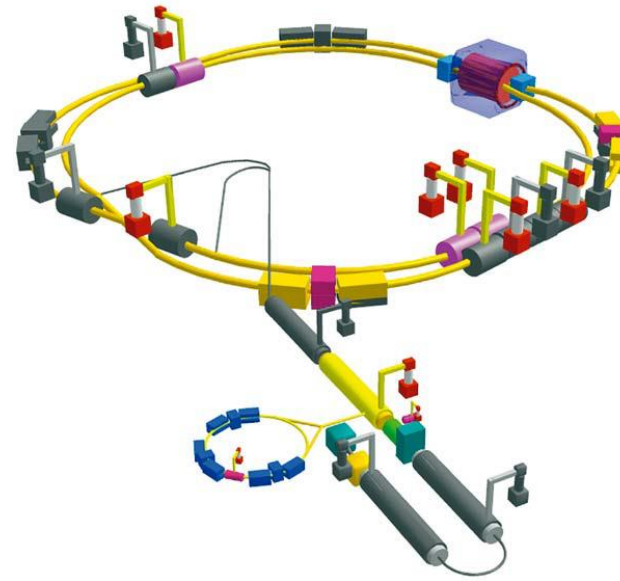




Super KEKB

40 times higher luminosity

Commissioning starts in January 2016

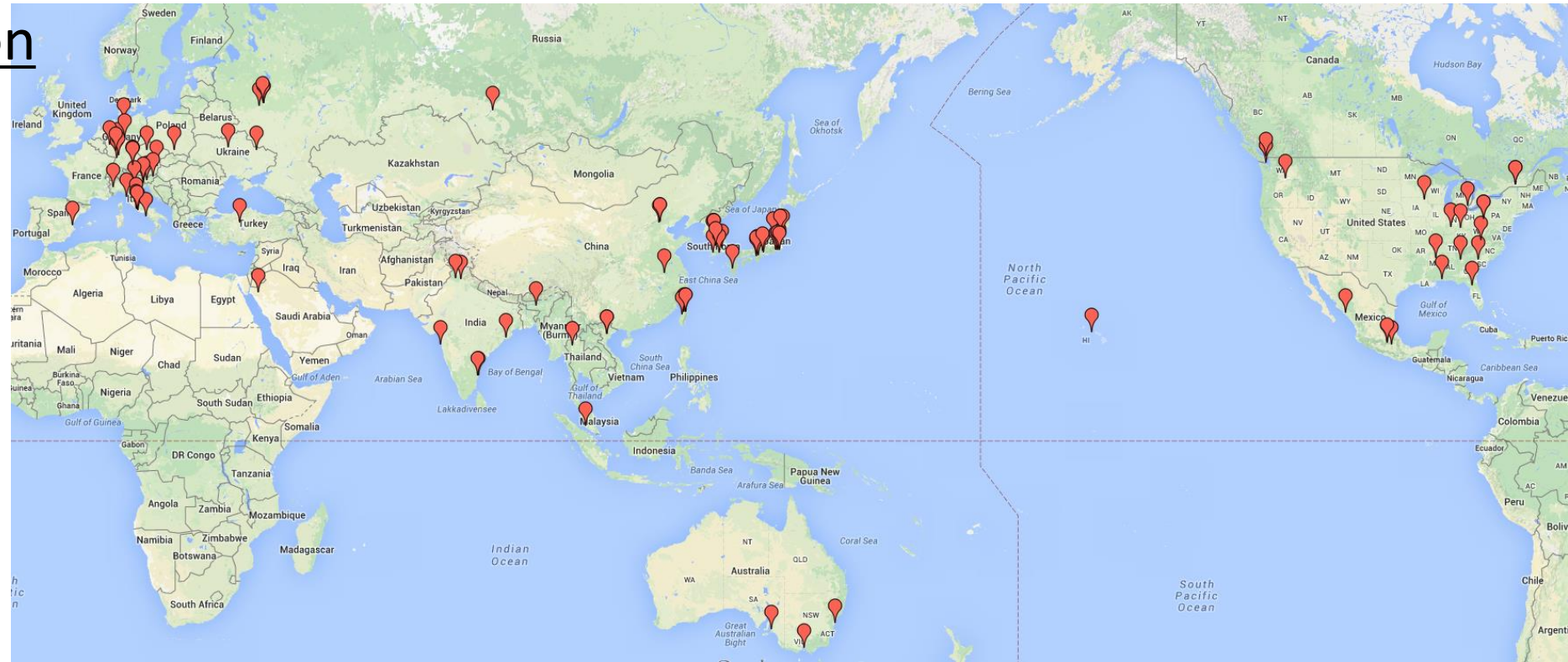


Belle-II Collaboration

23 countries/regions

99 institutions

>600 scientists



Big-Bang

The Universe was in a high-temperature high-density state

Particles and antiparticles coexisted



Pair annihilation



Matter was composed from remnant particles

$$\langle \mathbf{kT} \rangle \gg mc^2$$

$$\gamma + \gamma \rightarrow e^- + e^+$$

$$\gamma + \gamma \leftarrow e^- + e^+$$

How did number difference occur?

Sakharov's three conditions

- Baryon number non-conservation
- C and CP violation
- Imequilibrium

Present status of CP violation

- The standard model explains CP violation in both K-mesons and B-mesons
- The standard model, however, cannot explain the matter dominance of the Universe.
There will be yet unknown particles and unknown CP violating interactions.